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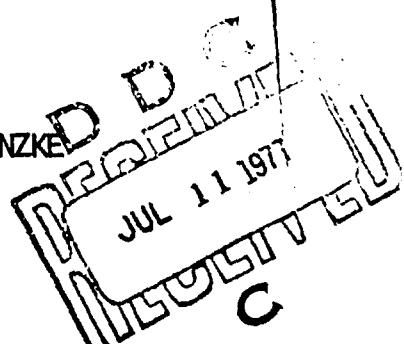
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IMPLEMENTATION OF RISK ASSESSMENT IN THE  
TOTAL RISK ASSESSING COST ESTIMATE (TRACE)

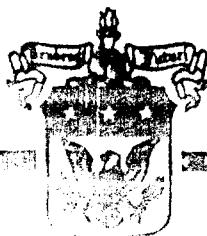
BY

LIEUTENANT COLONEL GENE A. VENZKE  
SIGNAL CORPS



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USAWC MILITARY STUDIES PROGRAM PAPER

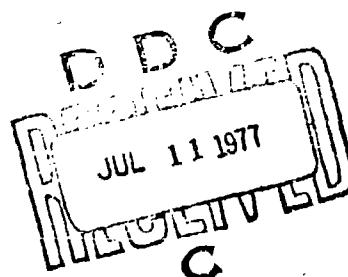
IMPLEMENTATION OF BLACK ARMY GROUP IN THE  
TOTAL REIN AGGRESSION COMB ESTIMATE (TRACE)  
AN INDIVIDUAL STUDY PROJECT

by

Lieutenant Colonel Gene A. Venkle, SigC

Colonel Robert T. Reed, AR

Study Advisor



US Army War College  
Carlisle Barracks, Pennsylvania 17013  
25 May 1977

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The concept of the Total Risk Assessing Cost Estimate (TRACE) was articulated by the ASA(R&D) on 12 July 1974. It is a means of explicitly accommodating the unforeseen and unidentifiable costs which characterize research and development projects. The TRACE is required to possess the property that it is an estimate of the 50th percentile of the project cost probability distribution. Unfortunately, early attempts to implement the TRACE met with limited success. A formalized study was undertaken to develop adequate techniques and two candidate methodologies emerged. One of the approaches, the TRACE Network Model, is extremely promising. The second technique, TRACE Risk Simulation, can be improved upon by a modification involving computer generation of the imbedded probability distribution. There remain some problems in "educating" users of the value of the TRACE, and the TRACE concept suffers from some inherent shortcomings. It is recommended that the new techniques for developing the TRACE be implemented, along with some ancillary actions to support the implementation and enhance the usefulness of the TRACE.

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## PREFACE

This Individual Study Project was undertaken as a part of the US Army War College Military Studies Program for Academic Year 1977. The study responds to a topic suggestion by the Deputy Chief of Staff for Research, Development and Acquisition (DCORDA), Headquarters Department of the Army. The author's choice of this topic was based upon experience with the problem at the Project Management Level combined with a continuing interest in improving the tools available to the Army for management of Research and Development projects.

During the research for this study, the author was privileged to secure the cooperation of individuals from 10 Project Management Offices (including 6 Project Managers), appropriate functional staff offices of three Major Subordinate Commands of the US Army Development and Readiness Command (DARCOM), as well as numerous personnel in DODCOM, within the DCORDA, other DoD Staff Agencies, and the Army Secretariat. The reader will find, however, no reference to specific individuals, as the information given was supplied on a non-attribution basis to encourage frank and forthright disclosure. Every effort has been made to insure honest and balanced presentation of the information collected.

The author wishes to express his appreciation to the above-mentioned personnel for their splendid cooperation; to C. John Blanchard, Jr., DARCOM, and to LTC Duane Riggs, USAF, for their in-process review of the paper; to his thesis advisor, Col Robert P. Reed, and to the other faculty members and fellow students who provided many constructive suggestions; and to the USAWC All System Development Center for their outstanding support.

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# **IMPLEMENTATION OF RISK ASSESSMENT IN THE TOTAL RISK ASSESSING COST ESTIMATE (TRACE)**

## **CHAPTER I**

### **INTRODUCTION**

Prior to developing techniques for implementing Risk Assessment, it is necessary to introduce some general concepts and definitions which will serve as the basis for detailed discussion. This chapter provides that background and introduces the problem.

#### **THE CONCEPT OF THE TOTAL RISK ASSESSING COST ESTIMATE (TRACE)**

It is relatively common knowledge that a serious problem in defense development programs is cost overruns and schedule slippage. Very few programs are completed within initial estimates of cost or within the time period initially projected for the development. Cost overruns of 50 or 100 per cent are not uncommon, as can readily be determined by perusal of newspapers or news magazines on an almost random basis. These overruns, in addition to creating adverse publicity and embarrassment, present a substantive problem -- to continue one project "grows", the funds to continue another project must come from deletion or deferral of

other projects of lesser priority. The net result is that the Army gets fewer of the systems on which plans were based, money spent on deleted systems is wasted, and deferral of other systems generally induces cost growth in those systems, thus creating a "snowball" effect.

On 12 July 1974, Mr. Norman Augustine, then Assistant Secretary of the Army for Research and Development, in a memorandum to the Director of the Army Staff (Annex A), directed that henceforth the concept of the TRACE would be used in Army Research and Development (R&D) Programs. The basic philosophy of the TRACE is as follows: Inherent in any R&D program is a factor of risk. Since R&D implies a foray into the unknown, it cannot be expected that every activity will occur according to plan. There will be blind alleys, unforeseen complications, and similar mishappenings. It is therefore unrealistic to allocate to a project only those resources which correspond exactly with the project plan. Additional funds must be programmed as a margin against those unforeseen and unidentifiable problems which characterize R&D projects.

The TRACE concept can be readily displayed in graphic form as shown in figure 1.

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TEACE MARGIN  
AN ALLOWANCE FOR  
UNFORSEEN AND UN-  
IDENTIFIABLE, BUT  
PROBABILISTICALLY  
EXPECTED PROBLEMS

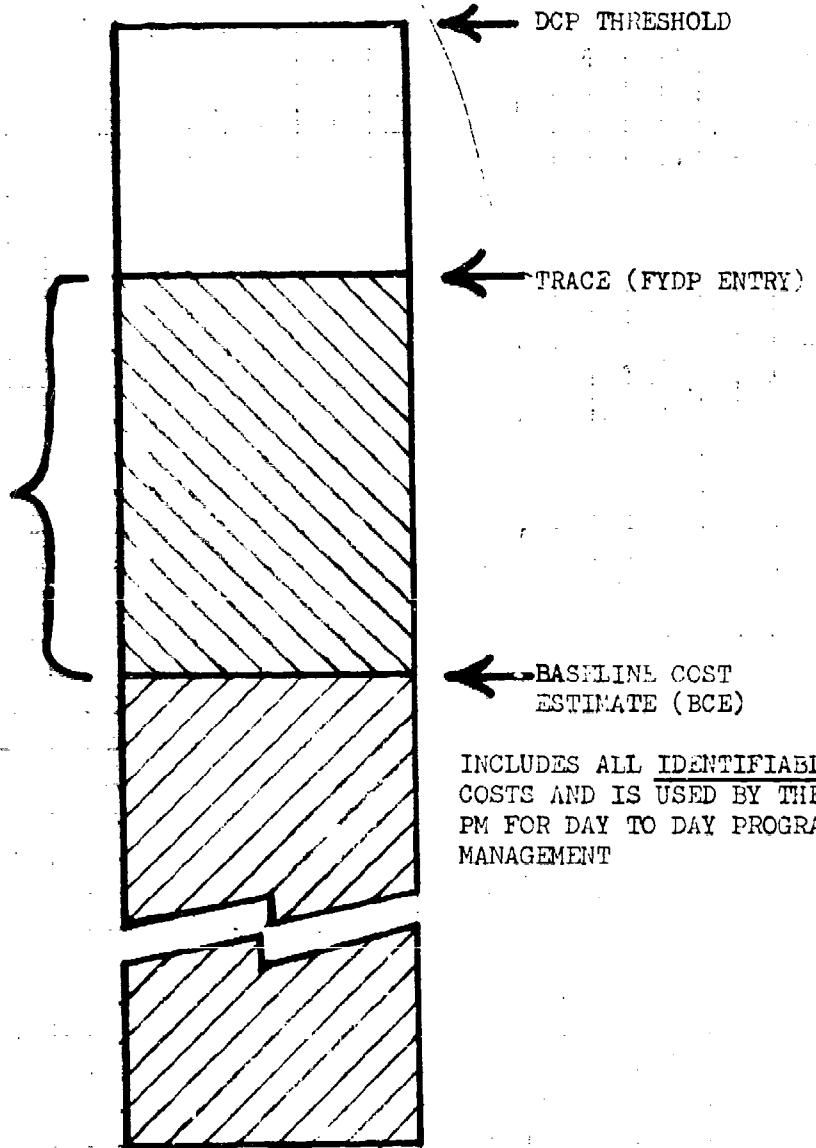


FIGURE 1

It should be noted that the Project Manager (PM) continues to use only the planned activities (Baseline Cost Estimate or BCE) as the project target cost, while the TRACE Margin is held at Department of the Army (DA) level in the Office of the Deputy Chief of Staff for Research, Development and Acquisition (DCSRDA) for release to the PM upon application and justification. However, the TRACE value is used for programming and budget purposes, and the cost entry in the Five Year Defense Program (FYDP) is the TRACE. Thus, the Army has fewer, but more realistically funded projects in the FYDP. After TRACE funds are exhausted, should that occur, the project may be continued through reprogramming, if desired, but is subject to challenge by higher authority to include action by the Defense Selected Acquisition Review Council (DSARC), should it appear that the Decision Coordinating Paper (DCP) threshold will be breached.

#### PROJECT COSTS AS PROBABILISTIC ENTITIES

To put the TRACE concept into a broader perspective, it is useful to introduce a probabilistic view of project costs. This view uses the notion that project costs follow a probability distribution such as figure 2.

## PROBABILITY DISTRIBUTION OF PROJECT COST

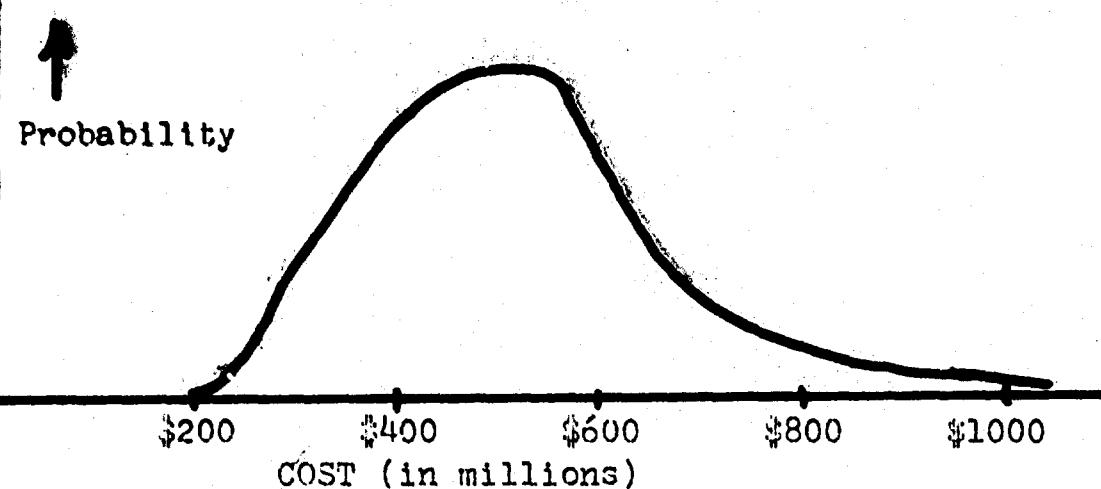


Figure 2

The probability distribution is interpreted by determining the area under the curve for any cost range of interest. For example, the probability that the project will cost less than a given amount is the area under the curve between zero and the given amount. Figure 3 illustrates this for \$400 million.

EXAMPLE FOR COST LESS THAN OR EQUAL TO \$400M

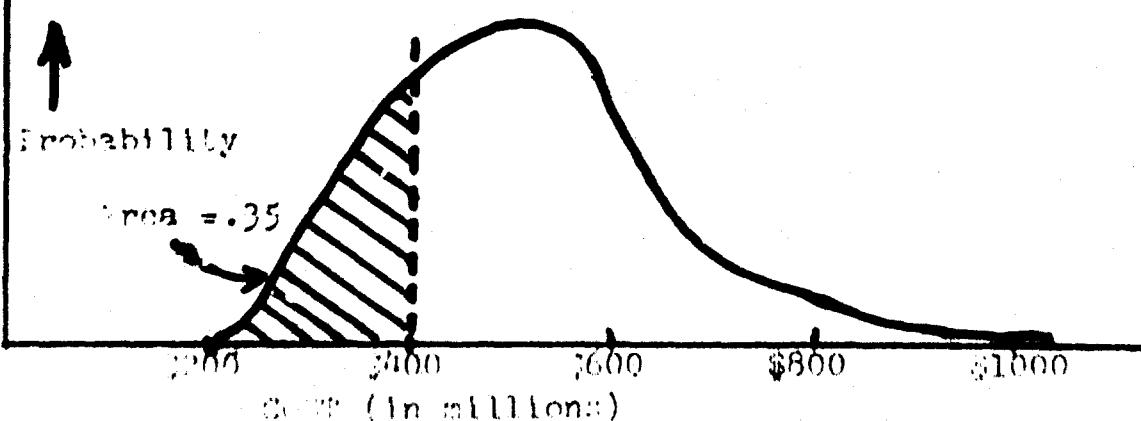
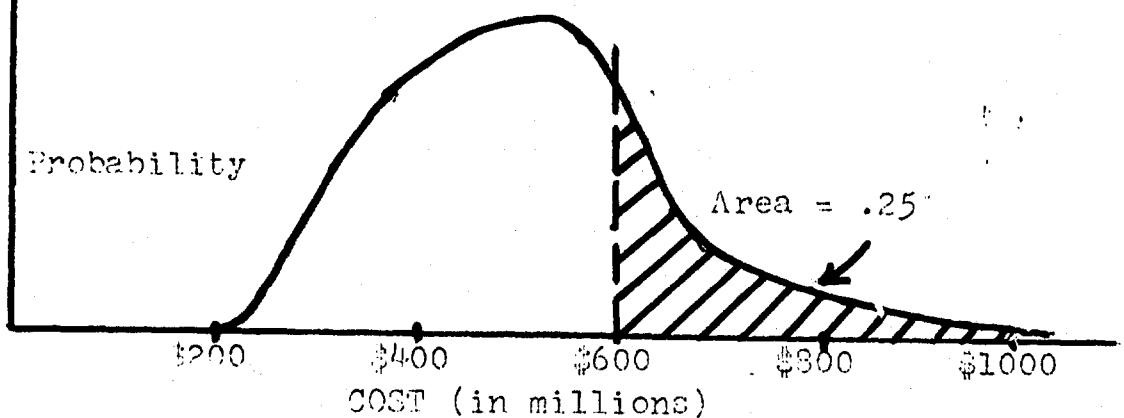


Figure 3

Since the shaded area in figure 3 is 0.35, it is determined that the probability of a project cost less than or equal to \$400 million is 0.35. By convention, \$400 million is called the 35th percentile of the distribution.

Similarly, the probability that a project will incur a cost greater than a given amount is found from the area under the curve to the right of the given amount. Figure 4 illustrates this for \$600 million.

EXAMPLE FOR COST GREATER THAN OR EQUAL TO \$600M



• Figure 4

From the probability of cost equal to or greater than \$600 million is 0.25.

Finally, figure 5 illustrates determination of the probability of cost within a specified range.

EXAMPLE FOR COST WITHIN A SPECIFIED RANGE

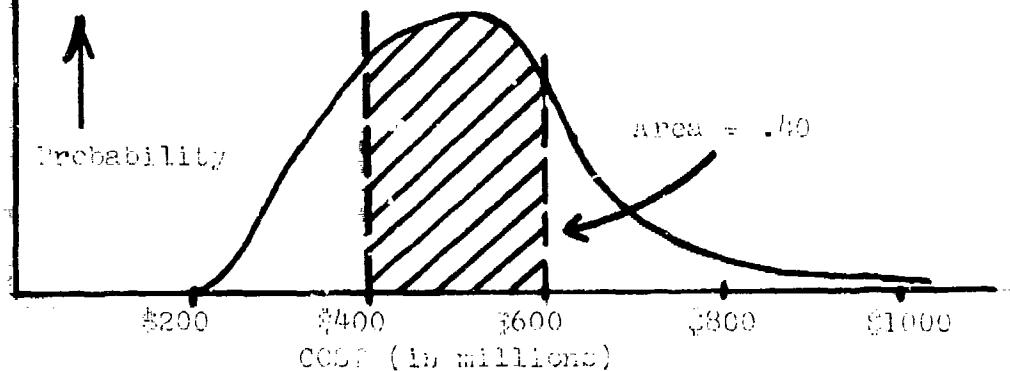


Figure 5

Here it has been found that the probability of project cost falling between \$400 and \$600 million is 0.40.

The foregoing, of course, is strictly theory. In practice, one does not have the probability distribution of project costs. At best, he may have an estimated or assumed distribution, but more typically he has even less information. Nonetheless, the probabilistic approach represents a convenient and meaningful basis for discussion, and a point of departure from which to gain some understanding of the real world situation.

THE TRADE IN THE PROBABILISTIC FRAMEWORK

Mr. Augustine, in his 12 July 1974 memorandum, actually used the probabilistic framework to define

the TRACE. Basically, he stated that the TRACE should be developed so as to represent the median, or 50th percentile of the cost probability distribution of a project. Figure 6 illustrates this concept.

PROBABILISTIC VIEW OF THE TRACE

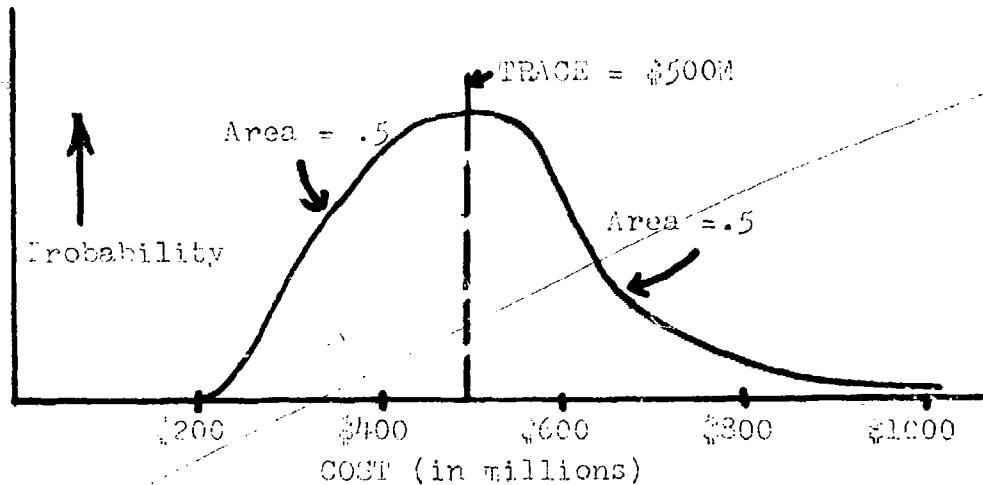


Figure 6

Thus there is a 50 per cent chance that the project will cost less than the TRACE (underrun) and likewise a 50 per cent chance that it will cost more (overrun). Mr. Augustine did not provide a rationale for selecting the median as the TRACE, but a reasonable rationale may be deduced as follows: The basic goal of the TRACE is to minimize the requirement to cancel or defer on-going or planned projects in order to fund overrun in other projects. By choosing the TRACE at the median cost

for each project, we achieve a solution where in the long run, about half the projects will overrun, while half will underrun. Overall, the money 'released' by the underruns should cover the cost of the overruns, and the necessity to disturb the programmed funds should be avoided.

If viewed in the short run, this rationale has some defects. Most significant is that in any given year, one may find that the overruns are all in the larger projects, while the underruns are in the smaller projects, resulting in a net shortage of funds. Obviously, the reverse could just as easily occur, with a resultant excess of funds on hand. If the state of the art of cost estimation permitted, one could actually adjust the TRACE percentiles (i.e., make the TRACE percentiles different from the median) on a project by project basis so that there would be a high probability of offsetting underruns and overruns. However, the state of the art of cost estimation does not support so ambitious an approach, and implementation of the median approach provides adequate challenge, as well as offering significant, if not ultimate improvement in reducing resource programming turbulence.

### TRACE DEFINITION

Unfortunately, in day to day use at various offices, the TRACE has acquired a large number of definitions and interpretations. For purposes of insuring clarity and understanding in this paper, and as a proposal for an overall definition to improve communication throughout the Army, the following definition of the TRACE is given:

"The Total Risk Assessing Cost Estimate (TRACE) is a point estimate, given in dollars, of the cost of a research and development project. The estimate is chosen such that the probability that it will be exceeded is 0.50. For control purposes the TRACE is normally divided into two parts -- the Baseline Cost Estimate (BCE), which includes both known and anticipated costs, and the TRACE Margin, which is a provision for the unknown and unidentified costs. The TRACE (and its components) may address the overall project cost, or the cost for a given Fiscal Year. If not clear from context, this distinction should be made explicit by identification, such as 'the FY80 TRACE' to indicate only one year, or 'the project TRACE' to indicate overall project cost."

### STATEMENT OF THE PROBLEM

The problem to be addressed in this paper is simply stated in the form of the question "How can the Army develop estimates of the cost of R&D projects which satisfy the requirements of the TRACE?"

## CHAPTER II

### CURRENT AND PREVIOUS TECHNIQUES

The problem is hardly new. There has been a continuing effort at all levels of management, both in industry and in government to improve the accuracy and realism of cost estimates over the years, and in fact, cost estimating techniques have improved. Unfortunately, the availability of resources (in real terms) has concurrently decreased, and the options for commitment of those resources have become more expensive. In short, the criticality of having a good cost estimate has outpaced the improvement in cost estimating techniques. Thus the challenge is to provide a cost estimating improvement which closes the gap. This chapter will discuss the approaches currently and previously used, and assess their success or lack thereof.

#### EXCURSIONS FROM THE BASELINE COST ESTIMATE

A number of techniques tried to improve the realism of cost estimates revolve around the use of the BCI as a point of departure and then developing an increment to cover potential cost growth. This is basically an attempt to develop the TRACE Margin as an isolated entity. Two

basically different subapproaches have been used.

#### Historically Based Excursion

One implementation of this technique was suggested by Mr. Augustine in his 12 July 1974 memorandum. It is commonly referred to as the "f" factor approach, although the derisive term "fudge factor" has also been applied. There are many variations, but a simple example will serve to demonstrate the technique.

Suppose the BCE for a new tank includes three major categories; automotive, armament, and fire control. From a review of past tank developments, the analyst determines that cost growth in those three categories has averaged 30 per cent, 40 percent, and 60 per cent, respectively. The current estimates in the three categories are then increased by the corresponding percentages. In practice, of course, considerably more detailed procedures are used, to include a lower level of detail, use of statistical procedures to validate the results, and integrating schedule considerations into the procedure to allow programming by Fiscal Year.<sup>1</sup>

These procedures suffer from a number of defects. First, the use of the BCE as a starting point introduces bias into the procedure right from the start. Second, the

extrapolation of growth factors from past developments is in itself a risky procedure<sup>2</sup>, and third, the cost/schedule relationships are not sufficiently well defined to facilitate proper programming.

#### Currently Based Excursions

The other general "excursion" technique, rather than extrapolating from past developments, attempts to use the current situation as the basis for estimating cost growth. Typically, Delphi<sup>3</sup> techniques are used to accomplish this task. The Delphi technique uses a poll of qualified experts to arrive at a consensus estimate. This approach can work well, but is very difficult to administer, and its validity is very sensitive to the proper structure of the poll, the expertise of the various experts polled, and the procedure used to reconcile variances among respondents. No case was found in the sample of projects used for this research where Delphi had been properly applied.

#### INDEPENDENT PARAMETRIC COST ESTIMATES

The use of Independent Parametric Cost Estimates (IPCE) to improve cost estimates is a well established procedure, and is required by regulation<sup>4</sup> in major programs. Unfortunately, in most cases, parametric

procedures are not sufficiently accurate nor do they provide adequate cost/schedule integration to serve as a basis for resource programming. They are, however, extremely valuable as a "cross check" and are regularly used to validate that a BOM is at least a " ballpark" figure. A wide variance between the BOM and IPCE is normally sufficient cause to require a re-evaluation of both estimates and a reconciliation of differences prior to proceeding. This use of the IPCE militates strongly against its use as an input to the TRAC. Should the IPCE be used in some way to develop the TRAC, or vice versa, the requisite independence of the IPCE will have been lost, and it will not be an effective "cross check" mechanism.

A final argument against using IPCE for the TRAC concerns the decreasing usefulness of parametric estimate with time. Typically, parametric estimates are most valuable when a project is in its embryonic stages, and the only well defined quantities are, in fact, the desired parameters of the product. However, as project definition proceeds, and design becomes firmer, manufacturing techniques proven, etc., engineering type estimates become more accurate and supersede the parametric estimates<sup>5</sup>. Ideally, the technique used to generate the TRAC should be viable throughout the project life.

## MANAGEMENT RESERVES AND RELATED TECHNIQUES

Historically, Project Managers have attempted to maintain a management reserve. Since management reserves are not generally authorized in the current environment, the PM endeavors to "bury" a de facto management reserve in one or more of the project activities. While this management reserve can be used to fund risk created setbacks, it can also be used to fund management errors and the like. Needless to say, while the Congress and the DOD may be willing to fund contingencies arising from the inherent project risk, they are quite unwilling to underwrite management mistakes. Thus the management reserve is not a suitable substitute for the PRACM Margin. Further, since management reserves are covertly included in the program, they are not based on a well defined estimating procedure, but are "seat of the pants" estimates made by the PM. These estimates are often referred to as "modified Delphi" -- inasmuch as they reflect the opinion of one "expert", the PM. The current climate within the DOD and particularly within the Army indicates that it will be increasingly difficult to arrange for a management reserve at the PM level. It appears that the PM will be well served in the future to develop a well supported PRACM Margin. It will be his only source of contingency funds.

## CHAPTER II

### FOOTNOTES

1. For an example of a more detailed approach see Letter, HQ, DA DAMA-PPM-P, subject: Letter of Instruction (LOI) for Implementation of RDTE Cost Realism for Current and Future Development Programs, dated 6 March 1975.
2. Bernard Ostle, Statistics in Research, pp.170-174.
3. J.W. Lanford, Technological Forecasting Methodologies; A Synthesis, pp. 20-23.
4. U.S. Department of the Army, Army Regulation 11-18, paragraph 2-3a, p. 2-6.
5. J.B. Holeman, Jr., A Product Improved Method for Developing a Program Management Office Estimated Cost at Completion, pp. 2-3.

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## CHAPTER III

### EVOLVING TECHNIQUES

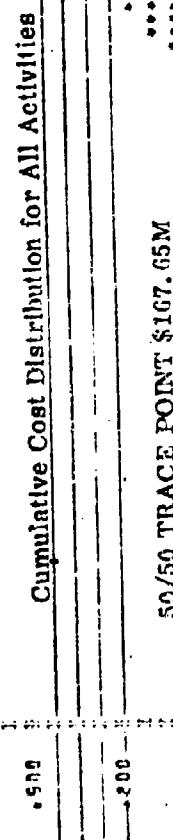
As a result of Mr. Augustine's memorandum and a subsequent DCSRDA Letter of Instruction (LOI)<sup>6</sup>, a number of techniques have been tried. The technique suggested in the DCSRDA LOI was generally found to be unworkable, as it was too general in nature and unfortunately, was also mathematically incorrect. PM Roland, through a contract with John M. Cockerham & Associates, Inc., developed a procedure which worked well for Project Roland. The contractor subsequently submitted an unsolicited proposal to document and generalize the procedure for use in a broader range of applications. This proposal was accepted and resulted in Technical Report RC-77-3, entitled US Army Total Risk Assessing Cost Estimate (TRACE) Guidelines.<sup>7</sup> This chapter consists of a short description of each of the two alternative techniques proposed in the report, along with a discussion of each.

#### TRACE NETWORK MODELING - DESCRIPTION

TRACE Network Modeling is named as the "preferred" methodology in the Cockerham report. It uses a Monte Carlo<sup>8</sup> simulation of the project activities to aggregate the overall effect of sub-estimates derived for each

activity. The technique is to break down the project into discrete activities which can be graphically arranged in a network to show their dependencies and interrelationships (e.g., testing cannot start until each of two competing prototypes are delivered, the test plan is approved, the range schedule is approved, and the instrumentation has been secured and calibrated). For each activity, an estimate is developed of three quantities -- the probability distribution of the fixed costs associated with the activity (e.g., the cost of test equipment), the probability distribution of the time required for the activity, and the probability distribution of the variable cost (cost per unit time) of the activity. The model is then "run" a large number of times, with a statistically valid value chosen at "random" from the appropriate probability distributions each time. Each "run" of the model is then one possible outcome for the project. All of the "runs" then constitute a large sample from which the overall project probability distribution can be estimated. Figure 7 is such an estimate, and is analogous to the probability distributions discussed in Chapter I. Since direct measurement of the area under the "curve" in Figure 7 would be difficult, the output shown in Figure 8 is also provided. It is simply the integral of Figure 7, so that





50/50 TRACE POINT \$167.65M

2.]

TRACCE DI SISTEMA

**COST-DISTRACTION FOR TERMINAL-NODE**—**90**  
**X-CAN**—**16650.95**  
**STANDARD-DEVIATION**—**64.86.55**

the area to the left of any point can be read directly from the ordinate on Figure 8. For example, to find the TRACE point, simply enter Figure 8 at the 0.5 ordinate and read the corresponding abscissa (.167.65).<sup>9</sup>

Another feature of the network model used by Cockerham & Associates is the ability to select outputs for a given Fiscal Year. Figures 9 and 10 show the two types of outputs for a given FY, and are most useful for assisting in making programming decisions.

#### TRACE NETWORK MODELING - DISCUSSION

The ensuing discussion of the TRACE Network Modeling technique is organized into three subsections -- advantages, disadvantages, and an overall evaluation.

##### Advantages

The requirement to break the project down into discrete activities forces a disciplined approach and allows the person(s) developing the various subestimates to work on a clearly definable entity. Since the network model accounts for many of the interdependancies between activities, the analyst can generally concentrate on the activity itself. Further, an estimating error in any one activity will have little effect on the overall result, and (hopefully), any estimating errors which are biased

1 0316 X

Cost Distribution for FY80

251

R 0284

221

190

150

125

95

63

32

32

32

32

32

32

32

32

23

TRACE RISK NETWORK

COST PRINTOUT FOR TIME = 12.60  
MEAN = 103463.51 STANDARD DEVIATION = 213.52

PROBABILITY OF COST LEVEL RUN AT TIME = 12.60 IS 100.00 AND THE AVERAGE IS 2163.51

FIGURE 9

1.000

1

0.900

1

0.800

1

0.700

1

0.600

1

0.500

1

0.400

1

0.300

1

0.200

1

0.100

1

0.000

1

### Cumulative Cost Distribution for FY80

• 600

1

• 500

1

• 400

1

• 300

1

• 200

1

• 100

1

• 000

1

• 000

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MEAN--100463.51

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### TRACE RISK NETWORK

on the low side will be offset by other estimates which contain a high side bias.

The network model integrates cost and schedule as an inherent feature of its function. The Fiscal Year output feature provides valuable programming information.

The output format (probability distribution) is extremely useful, and provides information not available from any other technique. Of particular value are the percentile estimates, the estimated variance, and the range of cost and schedule.

Once the model is developed, it can be readily modified and re-run to incorporate later information. For example, once the design phase is complete, the actual costs and schedule for the design phase can be inserted into the model, thus reducing the variance and sharpening the value of the estimate for the remainder of the project.

The model outputs provide a valuable framework for project monitoring. When the actual experiences of the real world deviate significantly from those indicated by the simulation, the PM can investigate to determine whether the problem is lack of realism in the model or a real world management problem. In either case, the PM can proceed on the basis of better information than he previously had.

The use of probability distributions rather than point estimates is a realistic representation of the real world. The normal probabilistic variations of real life are replicated in the model.

The model does not depend directly on the BCE as a point of departure. To the degree that inputs are developed independently of the BCE, the model results are free of any bias in the BCE.

#### Disadvantages

The usefulness of the output provides to the average user a feeling of accuracy and reliability not fully justified by the modeling process. The user is likely to forget that he is still dealing with an estimate.

The process of developing and running the model is expensive. It requires a competent analyst to properly develop the model and secure reliable estimates.

The model is basically just a technique for aggregating the activity estimates. It does not compensate for bad inputs -- the estimating problem has simply been "passed down" to the activity level. There is nothing in the procedure to assist in getting good activity estimates. In fact, the form of the required estimates (probability distributions) represents an unusual approach to most engineers and could lead to inadvertent errors.

Although the model takes into account most activity interdependencies, it cannot generally account for induced changes to follow on activities. For example, if the cost of activity 3 is dependent on the cost of activity 2, the model will nonetheless treat the two activity costs as independent. Special treatment by the analyst who develops the model may overcome some of these problems if the nature of the dependency is amenable to accommodation by the model.

Despite the complexity of the model, it still represents a considerable simplification of the real world. This simplification is achieved through various assumptions either explicit or implicit in the model. To the degree that these assumptions are not understood, not recognized, or not accounted for in interpretation of results, the model output may be misleading and inaccurate.

There is no simple technique for performing sensitivity analyses. Excursions from the baseline input require a complete rerun of the simulation.

#### Overall Evaluation

Of all the techniques currently in use, the TRACE Network Modeling Technique is by far the most comprehensive, and offers the most useful output, both in

terms of TRACE application, flexibility, and ancillary uses of output (such as for project monitoring). The Network Modeling Technique further has the potential to improve to the degree that network modeling and methods for developing better estimates of activity cost and schedules improve. Thus, where the project cost justifies the initial high cost of developing the TRACE Network Model, and where appropriate analytic and computer support is available, the Network Model offers the best approach to TRACE development.

#### TRACE RISK TABULATION - DESCRIPTION

The Cockerham report takes note that in some cases the Network Modeling Technique may be inappropriate. The TRACE Risk Tabulation technique is offered as an approach to be used in such cases. It may be characterized as an expected value simulation of the project, and like the network approach offers only an improved means of aggregating a number of sub-estimates, with no suggestion as to how those critical sub-estimates might be sharpened. The technique is best explained by reference to the tabulation (Figure 11, which is the example used in the Cockerham report). Step 1 involves reducing the project into elements suitable for analysis. The report suggests that a combination of Work Breakdown Structure (WBS)

**PROJECT Y**  
**WEAPON SYSTEM RISK ASSESSMENT**

Program Elements	Prob. of Occurrence P(A)	Cost Impact to Element/ Milestone	Prob. of Occurrence P(B A) P(B)	Cost/Schedule Impact to Other Program Elements			Date of Impact Calendar Date	Expected Loss	Adjusted Expected Loss
				TYPE A	TYPE B	TYPE C			
<b>Vehicle</b>									
1. Armor	.20	\$3.0M	-	-	-	-	4/78	.6M	.8M
2. Suspension	.60	\$ .4M	1.0	.60	\$1M, 2MN*	-	6/78	.84M	\$1.12M
3. Tracks	.25	\$ .8M	-	-	-	-	6/78	.2M	.27M
4. Power Train	.60	\$1.5M	.75	.45	\$4M, 2MN*	-	9/78	\$2.7M	\$3.6M
5. Engine	.20	\$ .5M	1.0	.20	\$ .5M, .1MN, Engines Qualification	-	9/78	.2M	.27M
6. Integration	.75	\$ .2M	1.0	.75	\$2M, 2MN*	-	11/78	\$1.65M	\$2.2M
<b>Program Milestones</b>									
7. Initiate Acceptance Testing	.70	0.0	1.0	.70	\$6M, 3MN*	-	2/79	.79	\$4.2M
8. OSD Review	.60	0.0	1.0	.60	\$2.5M, 1MN*	-	7/79	.79	\$1.5M
9. DSARC	.30	0.0	1.0	.30	\$4M, 2MN*	-	10/79	.80	\$1.2M
								<b>Totals</b>	<b>\$13.09M</b>
									<b>\$17.46M</b>

\*Total Program Schedule Slips

FIGURE 11

elements and critical milestones are best suited for the Risk Tabulation Model. The first column in figure 11 shows the results of step 1 for the example problem. Columns 2 and 3 are completed by securing (by Delphi techniques, presumably) the point probability and cost impact of likely overruns to the program element line. These are called "Type A" impacts and may be interpreted as follows: (line 1) "There is a 0.2 probability that the armor element will experience a cost overrun. If the overrun does occur, the cost of the armor will most likely be increased by \$3.0 million."

Columns 4,5,6 provide for interdependencies (Type B impacts). For example, on line 4, the column 4 entry of .75 means that if we do have problems with the power train, there is a .75 probability that other program elements will also be affected, and if they are, the overrun will be \$4.0 million with a two month schedule slip (col.6). The column 5 entry represents the overall probability that the column 6 impact will occur, and is computed as the product of the Type A and Type B probabilities (.60 times .75).

Columns 7 and 8 indicate the date and Fiscal Year of impact, to allow proper programming of TRACE margin funds. Column 9 is the expected value, defined as the probability of impact times the cost of impact. For line

4 the computation is .6 times \$1.5 million plus .45 times  
\$4 million = \$2.7 million.

Column 10 is an adjustment to the expected value of impact. This adjustment attempts to take into account the fact that if an impact does occur, it will cost the full impact value - not the expected value. Thus if the TRACE Margin were set at only the expected value of the impact, it is likely that the TRACE Margin would be inadequate.

The contractor provides an heuristic for making this adjustment. The rule is that any impact with overall probability greater than .75 will be fully funded, and those with lesser probabilities will use an adjusted expected value. For example, line 6, column 10 shows \$2.2 million (\$0.2 from col. 3 plus \$2.0 from col. 6). Since the probabilities are greater than (or equal to) 0.75, full funding has been used. Line 4 provides an example of the adjustment procedure when the probabilities are less than .75. Here the given probabilities are divided by .75 and the expected value is recomputed as (.6/.75) times \$1.5 plus (.45/.75) times \$4 = \$3.6. This adjusted value is justified on the basis of intuitive feeling and "reasonableness".

#### TRACE B104 TABULATION - DISCUSSION

As for the Network Modeling portion, this discussion

is organized into a listing of advantages, disadvantages and an overall evaluation.

#### Advantages

The technique is relatively inexpensive and readily easy to apply.

Updating is readily accomplished.

Sensitivity analysis is particularly simple since the contribution of any element to the mean can be analytically computed. For example, suppose we wish to examine the impact of changing the probability estimate for element 1 from .2 to .4. The new expected loss is \$1.2 million (.4 times \$3 million) and the adjusted expected loss is \$1.6 million (.4/.75 times \$3 million).

#### Disadvantages

The technique uses the BCC as a point of departure and is subject to the bias of the BCC.

The technique uses point probabilities of point costs as sub-estimates. This is a gross simplification of the real world and can lead to large errors.

The technique is highly dependent on the skill of

the analyst to identify and account for the various interdependencies.

The output is a point estimate which is always greater than the mean, but which cannot be related to the desired value of the TRACE (the median of the distribution).

Because the level of aggregation is high, the technique is quite sensitive to errors in the sub-estimates.

#### Overall Evaluation

In comparison with the Network Modeling Approach, the Risk Tabulation method appears weak, with the disadvantages far outweighing the advantages. However, in comparison to the previous techniques, it does provide a well defined, structured technique which forces a degree of disciplined analysis into the problem. For that reason it is preferred to earlier techniques. However, with minor modification, the TRACE Risk Tabulation method can be improved. A proposal for such improvement is presented in the next chapter.

## CHAPTER III

### FOOTNOTES

6. U.S. Department of the Army, Deputy Chief of Staff for Research, Development and Acquisition, Letter of Instruction (LOI) for Implementation of RD&E Cost Realism for Current and Future Development Programs, dated 6 March 1975.

7. As of the date of this report, a Defense Documentation Center (DDC) Catalog Number was not available. The cited report was the deliverable under Contract DAAM01-76-C-1012, IV Army Missile Command, Redstone Arsenal, Alabama, 35809.

8. Frederick F. Hillier and Gerald J. Lieberman, Introduction to Operational Research, pp. 450-460.

9. The network model used by Cockerham & Associates is proprietary to that firm. However the Army Logistics Management Center, Fort Lee, Virginia is currently modifying the Army's network model -ALICA (Army Information System for Cost((and Schedule)) analysis)- to provide the necessary features. Mr. Thomas A. Miller, Chairman, Decision Risk Analysis Committee, can provide up-to-date information on ALICA as well as other Army network models. (Commandant, US Army Logistics Management Center, ATTN: DRKOC-LC-CHD -Mr. Miller, Fort Lee, VA 23801. Autovon 637-4577.)

## CHAPTER IV

### A PROPOSED TECHNIQUE - RISK TABULATION/ EXPANSION

Two of the major disadvantages of the Risk Tabulation method are the use of point estimates as output and the heuristic adjustment of the expected values to get the final output. A modified technique is proposed which overcomes both these disadvantages.

#### PROBLEM FORMULATION

The initial formulation of the problem (figure 12) is the same as for the TRAC Risk Tabulation. However, the computation of the expected value and adjustment thereto is deleted. Instead, every simple computer program (Annex 1) is used to expand the program element estimates into their natural probability distribution, which is simply an estimate of the probability distribution of overall project cost.

#### COMPUTATION OF THE PROBABILITY DISTRIBUTION

Using the individual probabilities given in figure 12, the probability distribution is computed in a straightforward manner:

All possible combinations of impacts and non-impacts are enumerated and the associated probabilities

**PROJECT Y**  
**WEAPON SYSTEM RISK ASSESSMENT**

Program Elements	Prob. of Occurrence P(A)	Cost Impact to Element/Milestone P(B A) TYPE A	Prob. of Occurrence P(B A) P(B) TYPE A	Impact to Other Program Elements TYPE B	Cost/Schedule	Date of Impact Calendar Date
Vehicle						
1. Armor	.20	\$3.0M	—	—	4/78	78
2. Suspension	.60	\$ .4M	1.0	.60 \$1M, 2MN*	6/78	78
3. Tracks	.25	\$ .8M	—	—	6/78	78
4. Power Train	.60	\$1.5M	.75	.45 \$4M, 2MN*	9/78	78
5. Engine	.20	\$ .5M	1.0	.20 \$.5M, .1MN, Engine Qualification.	9/78	78
6. Integration	.75	\$ .2M	1.0	.75 \$.2M, 2MN*	11/78	79
<hr/>						
Program Milestones						
7. Initiate Acceptance Testing	.70	0.0	1.0	.70 \$6M, 3MN*	2/79	79
8. OSIR Review	.60	0.0	1.0	.60 \$2.5M, 1MN*	7/79	79
9. DSARC	.30	0.0	1.0	.30 \$4M, 2MN*	10/79	80

\*Total Program Schedule Slips

FIGURE 12

and costs are computed. As an example, one of the 768 possible combinations in the example problem (figure 12) is: no impact in elements 1,2,3,5,6, and 8; a type A impact in element 4; and type A and B impacts in elements 7 and 9. The probability of this combination would be computed as:  $(1-.2)(1-.6)(1-.25)(.6)(1-.2)(1-.75)(.7 \times 1.0)(1-.6)(.3)$  which is .000605. The associated cost is \$11.5 million, consisting of \$1.5 from element 4 (type A), \$.6 from element 7 (type A & B) and \$.4 from element 9 (type A & B).

After all possible combinations are evaluated, they are arranged in ascending order of cost, those combinations with equal costs are combined by adding together their probabilities, and a cumulative total of probabilities is also computed. Figures 13 and 14 display the results of the process for the sample problem. Figure 13 displays the input data for validation along with the mean, variance and standard deviation of the distribution, (these quantities are computed by the program as a side benefit), while Figure 14 is the listing of the distribution per se.

The computer program also produces two other output formats for special purposes. The first is a very detailed breakout showing each of the possible combinations of impacts along with the overall impact contribution (Annex C). This output is designed for the analyst who

### TRACE RISK TABULATION DISTRIBUTION

#### INPUT PARAMETERS

ACTIVITY	PROBABILITY OF TYPE A IMPACT	COST OF TYPE A IMPACT		CONDITIONAL PROBABILITY TYPE B IMPACT		COST OF TYPE B IMPACT
		3.00	0.	0.	1.00	
1	0.20	0.40	0.40	0.	1.00	0.
2	0.60	0.80	0.80	0.	0.	0.
3	0.25	1.50	1.50	0.75	0.75	0.
4	0.60	0.50	0.50	1.00	1.00	0.50
5	0.20	0.20	0.20	1.00	1.00	0.00
6	0.75	0.20	0.20	1.00	1.00	0.00
7	0.70	0.	0.	1.00	1.00	2.50
8	0.60	0.	0.	1.00	1.00	4.00
9	0.30	0.	0.	1.00	1.00	4.00

MEAN OF DISTRIBUTION 13.0900

VARIANCE OF DISTRIBUTION 22.177909

STANDARD DEVIATION OF DISTRIBUTION 4.709343

FIGURE 13

## DISTRIBUTION

CONST	PROBABILITY	CUMULATIVE PROBABILITY
0.	0.001613	0.0009507
0.4	0.000539	0.138647
1.0	0.000483	7.9
1.4	0.000419	0.000447
1.5	0.000405	0.15093
1.8	0.000134	7.9
2.0	0.000545	0.003467
2.3	0.000282	0.42560
2.4	0.000605	0.003610
2.5	0.002570	0.44170
2.9	0.000307	0.000680
3.0	0.002016	0.16851
3.2	0.001411	0.000222
3.3	0.000857	0.13171
3.4	0.000605	0.160022
3.5	0.000605	0.160579
3.6	0.007258	0.000557
3.7	0.002117	0.004559
3.8	0.000334	0.005138
3.9	0.000856	0.003452
4.0	0.002102	0.003259
4.3	0.000202	0.002732
4.4	0.003024	0.005482
4.5	0.000756	0.001798
4.6	0.001814	0.001223
4.7	0.000996	0.004691
4.8	0.000566	0.006217
4.9	0.000997	0.005415
5.0	0.000400	0.004284
5.1	0.0032722	0.002710
5.2	0.001411	0.237144
5.3	0.000050	0.005846
5.4	0.003154	0.000573
5.5	0.005287	0.005384
5.7	0.002117	0.000510
5.8	0.000133	0.006754
5.9	0.001134	0.003079
6.0	0.004166	0.0029322
6.1	0.011567	0.00733
6.2	0.015947	0.002142
6.3	0.000905	0.000454
6.4	0.000599	0.499363
6.5	0.002311	0.004619
6.6	0.001814	0.517424
6.7	0.000529	0.001265
6.8	0.001254	0.506693
6.9	0.007930	0.017842
7.0	0.003040	0.536935
7.1	0.002722	0.125
7.2	0.001399	0.125
7.3	0.000569	0.001392
7.4	0.006250	0.001265
7.5	0.001822	0.017842
7.6	0.007646	0.536935

13.7	0.022182	0.558717
13.8	0.000408	0.559125
13.9	0.010130	0.569255
14.0	0.009201	0.578456
14.1	0.002754	0.581210
14.2	0.001763	0.585973
14.3	0.000218	0.586191
14.4	0.001783	0.593974
14.5	0.007547	0.601521
14.6	0.037695	0.609216
14.7	0.014616	0.623832
14.8	0.002497	0.626329
14.9	0.001898	0.628227
15.0	0.001467	0.631694
15.1	0.022520	0.660214
15.2	0.004284	0.664498
15.3	0.000403	0.664490
15.4	0.013801	0.678702
15.5	0.006898	0.695600
15.6	0.006124	0.691723
15.7	0.002297	0.694010
15.8	0.000602	0.694712
15.9	0.011321	0.706033
16.0	0.001297	0.707330
16.1	0.018792	0.726122
16.2	0.028217	0.752340
16.3	0.000907	0.753247
16.4	0.005200	0.758447
16.5	0.001258	0.759705
16.6	0.005508	0.765213
16.7	0.004234	0.765447
16.8	0.000024	0.774771
16.9	0.010346	0.779118
17.0	0.009305	0.779123
17.1	0.002940	0.782063
17.2	0.007371	0.779434
17.3	0.000282	0.779636
17.4	0.019485	0.811581
17.5	0.001210	0.812791
17.6	0.033708	0.816499
17.7	0.009526	0.860224
17.8	0.000605	0.866620
17.9	0.001087	0.885117
18.0	0.05281	0.886106
18.1	0.005443	0.852421
18.2	0.000255	0.859496
18.3	0.001814	0.891096
18.4	0.013958	0.873454
18.5	0.003175	0.876629
18.6	0.009477	0.886106
18.7	0.002117	0.886223
18.8	0.01058	0.889281
18.9	0.001814	0.905119
19.0	0.000753	0.891849
19.1	0.012247	0.904096
19.2	0.006350	0.910446
19.3	0.000151	0.910598
19.4	0.007922	0.915119
19.5	0.000718	0.914236
19.6	0.000328	0.919356
19.7	0.000227	0.919792

FIGURE 14 (continued)

desires full visibility into specific combinations for detailed examination, such as evaluating probable time of impact for programming purposes. The second format aggregates the costs into broad cost bands for graphing, and will be further discussed later in the paper.

#### USE OF THE PROBABILITY DISTRIBUTION

The additional usefulness of the modified risk tabulation approach can be demonstrated by comparison of figures 13 and 14 with figure 11.

First, it should be noted that both methods provide a mean (expected) loss of \$13.09 million, which is to be expected since they use the same basic estimates. In figure 11, the heuristic adjustment to the expected value produced a TRACE Margin of \$17.46 million. However, reference to figure 14 reveals that \$17.46 million is at the 80th percentile of the distribution - - quite a deviation from the DA guidance to fund at the 50th percentile, and definitely an over-conservative approach.

From figure 14, it can be seen that the median cost estimate is approximately \$13.05 million. Therefore, adherence to the ASA(B&D) guidance indicates a TRACE Margin of \$13.05 million. Use of the modified approach in the sample problem then would have "freed" \$4.35

million ( $17.45 - 13.05$ ) for other programs, while maintaining the required probability of avoiding an overrun.

Should the situation demand deviation from the nominal AGA(RD) guidance, the probability distribution provides a solid basis for response. For example, should a project be one of high visibility, so that only a 40 per cent chance of overrun is desired, an estimate can be taken directly from figure 14 as the 60th percentile ( $\$14.45$  million for the sample problem).

Another use of the probability distribution is to provide a graphic display of the funding probability profile. The computer program has an optional output designed to facilitate graphing. This output (figure 15) merely combines all costs into bands which include those cost-within + 0.5 million of the stated value and computes the associated probability. In the sample problem, for example, the probability of a cost between  $\$11.5$  and  $\$12.5$  million is .089936, and the probability of a cost less than  $\$12.5$  million is .459035. The graph made from this output is shown in figure 16, and supplies a useful picture to complement the printed outputs. It can be seen that the bulk of the probability distribution is concentrated between  $\$10$  and  $\$18$  million, and that the

DISTRIBUTION

COST	PROBABILITY	CUMULATIVE PROBABILITY
0.0	0.001613	0.001613
1.0	0.003965	0.005578
2.0	0.009156	0.014734
3.0	0.005955	0.020530
4.0	0.019448	0.039978
5.0	0.025307	0.065285
6.0	0.028980	0.094166
7.0	0.027328	0.121494
8.0	0.052377	0.174370
9.0	0.045840	0.220210
10.0	0.072786	0.292996
11.0	0.076053	0.369048
12.0	0.089986	0.459035
13.0	0.059588	0.518693
14.0	0.082328	0.601521
15.0	0.084079	0.685600
16.0	0.074106	0.759705
17.0	0.043085	0.802791
18.0	0.073388	0.876629
19.0	0.042009	0.919238
20.0	0.022335	0.941372
21.0	0.02042	0.961614
22.0	0.023701	0.985315
23.0	0.00766	0.993281
24.0	0.001146	0.994727
25.0	0.004253	0.996979
26.0	0.001021	1.000000

FIGURE 15

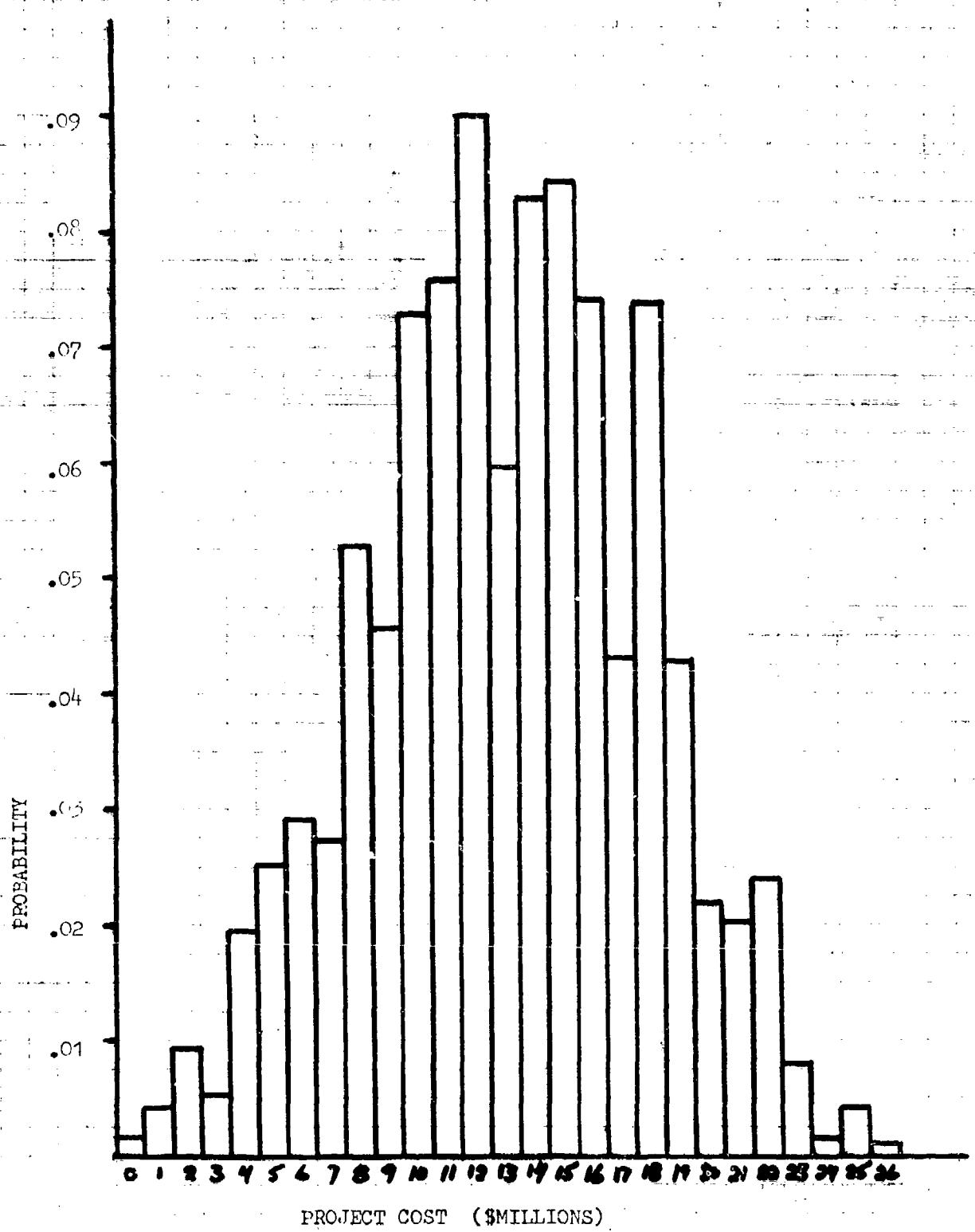


FIGURE 16

most likely overrun is in the \$11.5 - \$12.5 million cost band. Thus, the 50th percentile value of \$13.05 million not only meets the DA guidance, but also includes the most likely overrun value, which provides some measure of comfort. In general, the graphic display shown in figure 16 provides a good quick picture of the cost probability distribution for management level evaluation, with the more detailed computer printouts available for analyst level activity.

#### DISCUSSION OF THE PROPOSED APPROACH

The TRAC3 Risk Tabulation/ Expansion approach is not proposed to replace the Network Modeling technique. Certainly, where the size of the project and availability of supporting resources justify its use, the Network Model should be used -- it is "state of the art". However, where the Network approach does not seem justified, or is not feasible, the TRAC3 Risk Tabulation / Expansion provides considerably greater utility and project visibility than any of the other approaches.

#### FURTHER REFINEMENTS

The TRAC3 Risk Tabulation/ Expansion technique can be expanded to provide more definitive programming (i.e., time-phasing) information. The general approach

is to divide the program elements into subsections by fiscal year, and then to expand the probability distributions for both cost and schedule each year. This will provide a more convenient basis for per year allocation of TRACO Margin funds.

## CHAPTER V

### GENERAL OBSERVATIONS ON TRACE IMPLEMENTATION

During the course of researching this paper, the author had contact with a broad cross-section of personnel associated with the implementation of the TRACE concept, ranging from Mr. Augustine down to cost analysis personnel within commodity commands and Project Management Offices. The observations made, while not of direct application to the topic at hand, seem to merit documentation. This section will list those observations.

#### SUPPORT FOR THE TRACE

Generally, the TRACE concept is well supported at Headquarters, DA, and at Headquarters, US Army Development and Readiness Command (DARCOM). At the DARCOM subordinate command level, support is spotty, and at PMO level, with some exceptions, TRACE is intensely disliked. Typical PMO comments follow:

"TRACE is a meaningless exercise in obfuscation."  
"TRACE simply deprives me of funds I should have -- I know that Project Y is in trouble and I will lose my TRACE Margin funds to PM Y." "No matter what anyone says, the TRACE Margin is a management reserve and the PM needs that reserve, not DODRDA."

Overall, it appears that firms are complying with the requirements for the TRACI Margin only because it is required, and that the compliance is, in general, done very begrudgingly. (There are, it is emphasized, a few exceptions who vigorously and enthusiastically support the TRACI concept.)

#### UNDERSTANDING OF THE TRACI

Generally it was found that the TRACI concept was understood by working level personnel at all levels. However, at the management level, there are as many different interpretations of the TRACI as there are managers. Specifically, there appears to be a lack of understanding of the distinction between TRACI Margin and Management Reserve, a failure to recognize that some overruns are expected, as well as underruns, and lack of understanding of the rationale for maintaining high level control of TRACI Margin funds. In a number of cases, firms are demonstrating their misunderstanding of TRACI by attempting to prograde the use of TRACI Margin funds.

#### IMPLEMENTATION OF TRACI

Overall, the initial implementation of TRACI was "most of the parts" -- again with a few exceptions.

When faced with the requirement to designate a TRACI Margin, most MIs simply couplied up all or a portion of their management reserve and relabeled it TRACI Margin. It does appear that newer projects and those ongoing projects which are being restructured, are doing a better job of complying with the TRACI concept.

#### Shortcomings Of The TRACI Concept

Notwithstanding the progress being made in improving TRACI implementation, it must be recognized that there are a number of shortcomings inherent in TRACI per se (as opposed to those peculiar to specific implementation techniques). These are listed below in outline format.

##### Incompatibility with PP's

The requirement to program funds on a fiscal year basis places a severe constraint on TRACI. Ideally, the TRACI Margin should be funded on an any year basis, so that unused funds in one year could be carried over to support potential problems in later years, or conversely, so that funds would be available to cover high overruns in the early years, hopefully to be offset by underruns in later years. (This problem is hardly unique to TRACI, but is highlighted by the impact it has on TRACI).

The requirement to include TRAC Margin funds in the PMS line items (project element lines) creates two problems:

It defeats the basic thrust of PMS -- that the savings accrued in those 50% of the projects which under-run can offset the overruns in the other 50% of the projects. This can be done now only through reprogramming (in general), which subjects the available funds to possible withdrawal by higher authority.

It allows contractor knowledge of actual fund availability. Since contractors have access to line item totals, they can readily estimate the actual money available to them by subtracting out the total government "in-house" costs, which are fairly easy to estimate. Thus the PAs efforts to stay within their ACD may be thwarted by contractor knowledge of the amount of additional funding actually available.

One possible solution to these problems is to create (assuming necessary statutory/regulatory approvals) a separate contingency line, in which all TRAC margins are carried, and thus lose their project identity. This solution would help greatly with the fiscal year programming problem since cross reimbursement on a free basis in any given year would ameliorate many of the multi-year problems. However, its effect on the contractor

knowledge situation is difficult to assess. Now the contractor does not see the TRACCS Margin allocated to his risk, but he does see the overall pool, and must estimate how much is his "share". The question now is -- will he overestimate or underestimate his "share"?

Discussion of that question is beyond the scope of this paper, but it is clear that if a few contractors were to overestimate, severe problems would ensue.

A further consideration in adoption of TRACCS Margin "pooling" is that of possible higher echelon pooling. If the Army could present adequate argument to secure permission to "pool", that argument would tend to support and even encourage a grand pool at DOD level, thus denying the Army the flexibility sought in the first place.

#### Treatment of Technical Risk

All the techniques thus far derived for TRACCS implementation do not explicitly treat technical risk, but instead focus on cost and schedule risk, with technical risk being at best an implicit factor. This approach is natural, since cost growth and schedule slippage are indeed the principle manifestations of technical risk. Nonetheless, it appears that more explicit treatment of technical risk could add to the usefulness and validity of the TRACCS.

### Inflexibility in TRACE Margin Administration

This problem revolves around bureaucratic inflexibility in releasing TRACE Margin funds to I'Ms. Because the various directives pertaining to TRACE speak specifically to using TRACE Margins to fund overruns of the BCE, I'Ms are not being encouraged to use their available TRACE Margin funds to prevent future overruns. For example, there appears to be a philosophy that FY77 TRACE Margin funds can only be used to pay for overruns which require FY77 dollars. In fact, a more efficient use of those funds, if they are not required to pay for current overruns, is to fund necessary activities to prevent future overruns. Generally speaking, funds used in the "overrun prevention" mode will provide much greater return than those used in the "overrun compensation" mode. Care must be taken, of course, that proper and complete justification is provided, and that the use of TRACE Margin funds for overrun prevention is in response to newly identified problems (as opposed to previously known problems which could have been resolved through the normal programming process).

## CHAPTER VI

### RECOMMENDATIONS

It is recommended that:

The TRACI Risk Tabulation/ Expansion Technique be established as the minimum acceptable approach to TRACI implementation.

The TRACI Network Modeling Technique be used whenever project size available support make it possible.

Additional emphasis be placed on using the TRACI structure as a management tool for monitoring and controlling the project. The TRACI should be updated as significant events are completed as well as routinely, on a calendar basis.

Work be expedited to implement a TRACI Network Modeling capability on existing Army Network models such as BTCCA.

Additional work be done to improve the realism and treatment of interdependencies in Army Network Models, to provide a technique for extracting outputs by fiscal year, and to provide explicit schedule risk outputs.

Additional instruction on detailed TRACI methodologies be incorporated into the Program of Instruction at the Army Logistics Management Center and related

schools.

The inclusion of explicit consideration of technical risk in TRACE methodology be evaluated.

The administration of TRACE Margin funds be redirected to encourage PMs to use available TRACE Margin funds to prevent future overruns as well as pay for current overruns.

SELECTED REFERENCES

1. Galle, Bernard. Statistics in Research. Ames: The Iowa State University Press, 1963. (IA29 C8)
2. Hillier, Frederick S. and Lieberman, Gerald J. Introduction to Operations Research. San Francisco: Holden Day, 1967. (Q180 AL174R C.2)
3. Wiener, Gene H. Cost Considerations in Systems Analysis. New York: American Elsevier, 1971. (RAND R-490 ADD C.10)
4. Lanford, R.W. Technological Forecasting Methodologies: A Synthesis. American Management Assn., 1969. (T124 135)
5. The Rand Corporation. Military Equipment Cost Analysis. Santa Monica: 1971. (RAND Z-MECA C.14)
6. Summers, Robert. Cost Estimates as Predictors of Actual Weapon Costs: A Study of Major Hardware Articles. Santa Monica: The Rand Corporation, 1962. (RAND RK-3061-PR)
7. Dalkey, Norman C. Dekuki. Santa Monica: The Rand Corporation, 1962. (RAND P-3074 C.5)
8. Holoman, J.B. Jr. A Product Improved Method for Developing a Program Management Office Estimated Cost at Completion. Fort Belvoir: Defense Systems Management School, 1975.
9. John T. Cockerham and Associates, Inc. U.S. Army Total Risk Assessing Cost Estimate (TRACE) Guidelines. Hopewell: 1976.
10. US Department of the Army, Deputy Chief of Staff for Research, Development and Acquisition. Letter of Instruction (LOI) for Implementation of Cost Realism for Current and Future Development Programs. Washington: March 1975. (DAM-PTM-P)
11. US Department of the Army, Army Regulations 11-13: The Cost Analysis Program. Washington: October 1975.

ANNEX A



DEPARTMENT OF THE ARMY  
OFFICE OF THE ASSISTANT SECRETARY  
WASHINGTON, D.C. 20310

12 JUL 1974

MEMORANDUM FOR THE DIRECTOR OF THE ARMY STAFF

SUBJECT: RDT&E Cost Realism -- Future Development Programs

One of the strongest criticisms leveled against the Department of Defense in recent years has, I believe, related to the difficulty of controlling the costs of development activities. The present memorandum addresses development costs; however, the action proposed could equally apply to the estimation of production "design-to" costs.

It is noted that the problem in the past has not been the need of a method for fine-tuning cost estimates to, say, the nearest 2 or 3 or even 10%. Rather, the problem has been one of finding a means of avoiding gross errors on the order of 50 to 100% and more. We have rarely, if ever, had an underrun on a major program. However, it is not our objective to establish program cost estimates so high that there would be underruns in a large majority of cases. Our estimate should be unbiased so that we have about an even chance of either going over or under it.

It is submitted that cost overruns will continue to be a way of life until adequate recognition is given to the impact of program uncertainty in estimating costs. There are, of course, many types of uncertainties that influence program costs, such as unforeseen program changes, inflation, inaccurate cost estimating, technical problems, threat revisions, etc. It is particularly important for the Army to improve our capability as a "sophisticated buyer" in the analysis, evaluation and validation of program proposals by industry.

RDT&E cost estimates have traditionally been based on an approach which compiles expected costs for specifically identified tasks. It is, of course, important that we continue to refine our ability to identify those essential tasks and to prepare plans for their efficient accomplishment. Beyond this, it remains the fundamental nature of RDT&E, wherein by definition one is producing a particular item for the first time, to involve the unknown. These unknowns invariably lead to cost

requirements which cannot be individually foreseen at the outset of a development -- yet their cumulative impact can be seen in retrospect with all the assuredness of the laws of probability. The record shows a major factor in properly estimating RDT&E cost is, therefore, to assess realistically the probable gross extent of the unknowns in a program in advance -- i.e., the certain uncertainties.

The lessons of history strongly suggest that even the most capable program manager is not able to forecast all the problems which will be encountered in a development program which typically spans six to ten years into the future. It is, however, quite possible to conduct a risk analysis and thereby forecast, statistically, the probable additional funds which will be required to overcome these certain uncertainties. The provision of flexibility in the funding plan for such purposes does not represent the creation of a "slush fund," or a "reserve" (in the usual context), but rather merely gives due recognition to the fact that unanticipated problems always have, and always will, arise even in the best managed RDT&E programs ... and that our base-line cost estimates should reflect these probable additional costs.

The provision of additional planning funds commensurate with the assessed risk in proposed programs does, of course, mean that the effort to justify these new programs will be more difficult. Similarly, it will not be possible to start as many new programs if they must all fit into a given out-year budget projection. On the other hand, it seems far preferable to recognize these realities at the outset rather than part way through a development at which time cost growth in one program can often be compensated only by the inefficient mechanism of cancelling still other partly completed programs.

It is, therefore, proposed that a Total Risk Assessing Cost Estimate (TRACE) be generated for all future development programs and used as the basis for justifying those programs. The TRACE estimate is defined as one having a 50:50 chance of producing either an overrun or an under-run. One possible method of aggregating the TRACE estimate is:

- (1) A "risk factor" would be assigned to each element of the program's work breakdown structure (probably a three-level structure is adequate for this purpose and should be available early in the program). A risk factor of 1.0 would correspond to a routine task with no risk

whatsoever. A factor of 1.3, for example, would characterize an effort wherein experience indicates that tasks which are not explicitly definable at the outset will most probably exceed those which are, in fact, definable by an expected value of about 30%. (The actual magnitude of the risk factor can generally be determined by a comparison of the degree of departure of the proposed task from corresponding tasks which have been accomplished in the past and by an assessment of the uncertainty which exists in the performance demanded of the item.)

(2) The risk factor would be multiplied by the basic cost estimate for the known efforts to be performed in each element of the work breakdown structure. An aggregate of these weighted costs would then provide a cost estimate for the program which recognizes the certain uncertainties which invariably arise in a development program.

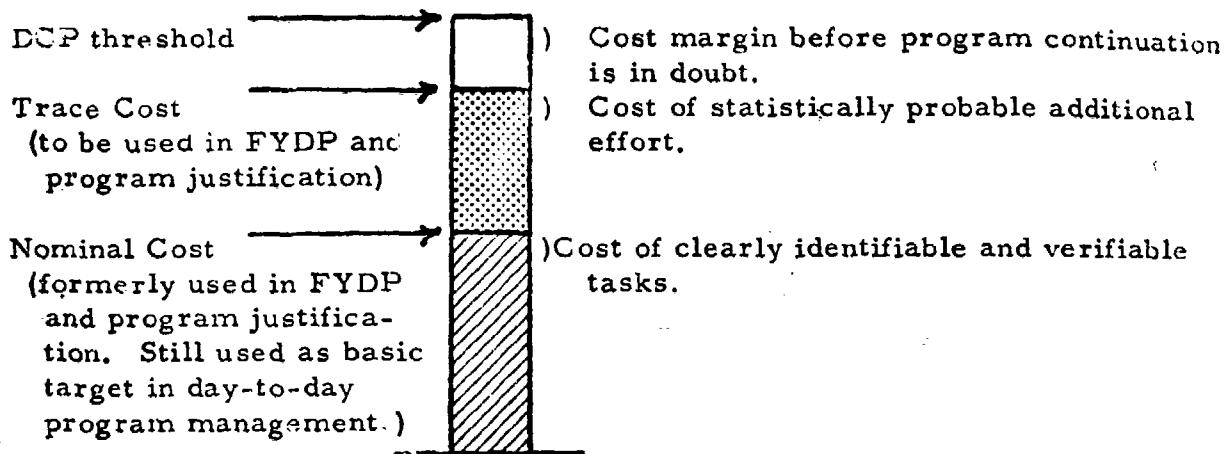
(3) The TRACE estimate would make use of all supportable estimating techniques such as Independent Parametric Cost Estimating (IPCE).

(4) The forecast of fund requirements which has been defined after consideration of uncertainties in the above manner would generally (although not necessarily always) be included in the latter years of the development funding plan. By so doing it is not necessary to justify the budget of these funds to Congress in a given year until the specific reason for needing them has, in fact, become known. Further, if, by the law of averages, some of the funds on an individual program are not ultimately needed, they can simply be dropped from the then-year budget request before it is submitted to Congress.

(5) The development activity would continue to be managed on a day-to-day basis against the nominal cost estimate (i.e., without risk funding), making the additional funds available to the Project Manager only when formally requested and adequately justified.

(6) All new R&D programs will be discussed with the user and justified to OSD and to the Congress using the TRACE figure (i.e., the cost estimate including the expected impact of risk). Program threshold cost estimates in the DCP would be no less than the TRACE estimate and generally greater.

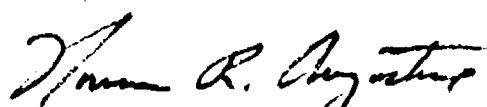
This concept is shown schematically in the following sketch:



In summary, it should be emphasized that the approach proposed herein is not one of creating unverified contingency funds or slush funds or self-fulfilling cost estimates. To the contrary, it merely gives recognition to the established fact that every individual funding demand which will arise in a 6-10 year development effort simply cannot be explicitly identified in advance -- but that the aggregate of those demands can be reasonably predicted and should, therefore, be included in program planning.

It should be noted that the problem being addressed herein is related to, but intentionally separated from, the also very difficult problem of predicting inflation. This latter task need not be allowed to complicate the matter considered herein of properly accounting for those factors which are largely within the control of program management.

Unless you have some objection to the policy and procedures expressed above, please have them implemented in appropriate Army materiel acquisition directives.



Norman R. Augustine  
Assistant Secretary of the Army  
(Research and Development)



SECRETARY OF THE ARMY  
WASHINGTON

July 12, 1974

MEMORANDUM FOR THE CHIEF OF STAFF

SUBJECT: RDT&E Cost Realism -- Current and Future  
Development Programs

Past experience in the acquisition of major weapons systems indicates that we generally exceed our initial cost estimates ... sometimes by as much as 100% or more. This problem, of course, is not unique to the Army. However, to prevent misleading the decision makers who approve our programs, we must produce more accurate cost estimates for the development of our major weapons systems.

The accuracy of our major program cost estimates is influenced by many factors including inflation, poor estimating, changing requirements, technical risk, etc. Risk is inherent in any research and development program and, generally, the greater the risk, the greater the potential payoff of the program. Unfortunately, there also appears to be a direct correlation between the degree of risk and the difficulty of producing accurate cost estimates.

While we cannot eliminate all technical risk from our programs nor precisely predict specific problems that will occur, we can, from past experience, assess their impact statistically and consider this in our RDT&E program plans. The problem of generating RDT&E cost estimates that more accurately reflect probable outcomes has undergone a review by elements of the Secretariat and the Army Staff and a revised policy has resulted. Under this revised policy we would no longer follow the practice of programming based only upon those tasks which can be clearly foreseen at the outset of a program and which therefore do not allow for uncertainty. By applying this Total Risk Assessing Cost Estimate (TRACE) approach, I am convinced that we can provide more accurate data in support of our programs at the OSD and Congressional levels. I have asked the ASA(R&D) to provide the details of the TRACE concept directly to your staff and would be appreciative of your helping implement this policy guidance.

  
Howard H. Callaway

ANNEX B



DEPARTMENT OF THE ARMY  
OFFICE OF THE CHIEF OF STAFF  
WASHINGTON, D.C. 20310

5 August 1974

MEMORANDUM FOR: SECRETARY OF THE ARMY  
SUBJECT: RDTE Cost Realism -- Current and Future Development Programs

We have begun the process of implementing the policy of RDTE cost realism enunciated by you and Assistant Secretary Augustine in your 12 July 1974 memoranda. Your policy will receive high visibility here and in the field.

For each current development program qualifying for decision by the ASARC, the Chief of Research, Development and Acquisition is requesting a one-page review from the materiel developer. Each review will show what changes would be needed in a program to provide 10% and 20% margins of estimated funding from FY76 to completion of development. These reviews will be evaluated at HQDA by 30 September 1974 for the purpose of making specific program recommendations.

For future development programs, the Chief of Research, Development and Acquisition, working with the Comptroller of the / (Director of Cost Analysis), will issue a letter of instruction on 1 October 1974. This will be an interim document to implement your policy, pending revision of Army regulations.

*Fred C. Weyand*  
FRED C. WEYAND  
General, United States Army  
Vice Chief of Staff

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D010*#RUN *#/RAND/RUNY(ULIB,RCORE=24K,REMOLLIBRARY/USERLIB.R
0020 DIMENSION A(9),B(9),D(9),E(9)
0030 DIMENSION PROB(1000),NSTL(1000),INDIC1000,9),P(9,1)*C(9,3),
0040 READ IN BASIC VALUES. A(1)=PRNB OF TYPE A COST FOR THE
0050C 1TH ACTIVITY. B(1)=PROB OF TYPE B COST FOR THE 1TH
0060C ACTIVITY. D(1) = AMOUNT OF TYPE A COST. E(1) = AMOUNT
0070C DF TYPE B COST
0080 CALL FPARAN ( 1 , 132 )
0090 CALL CREATE(21,30000,0,1STAT)
0100 LRATE1 21 * 9060
0110 PRINT,"ENTER A PROB. A COST. B PROB. B COST"
0120 DD 65 I=1,9
0130 READ, A(I), B(I), D(I), E(I)
0140 WRITE(21,90101),A(I),B(I),D(I),E(I)
0150 CONTINUE
0160 PRINT,"ENTER 10PTN"
0170 READ,T0BT
0180 IF T0PT = 1 PRINT COMPLETE DISTRIBUTION WITH INDICATORS
0190 IF T0PT = 2 PRINT COMPLETE DISTRIBUTION W/O INDICATORS
0200 IF T0PT = 3 PRINT ABBREVIATED DISTRIBUTION
0210 DD 7 I=1,9
0220 P(I,1)=((1+I)*0 -B(I))
0230 P(I,2)=A(I)*B(I)
0240 P(I,3)=1.0-A(I)
0250 C(I,1)=D(I)
0260 C(I,2)=B(I)+E(I)
0270 ↑ C(I,3)=0.0
0280 IND=0
0290 EXPECT = 0.
0300 VAR = 0.
0310 DD 10 I=1,3
0320 DD 10 J=1,3
0330 DD 10 K=1,3
0340 DD 10 L=1,3
0350 DD 10 M=1,3
0360 DD 10 N=1,3
0370 DD 10 IJ = 1 : 3
0380 DD 10 JK = 1 : 3
0390 DD 10 KK = 1 : 3
0400 IND=1ND+1
0410 PROB(IND)=P(I,1)*P(2,J)*P(3,K)*P(4,L)*P(5,M)*P(6,N)
0420 ↑ P(I,1)*P(2,M)*P(3,J)*P(4,K)
0430 IND=IND+1
0440 GO TO 10
0450 IND=IND+1
0460 DD 10 I = 1 : 13 . 13 ) , 10PT
0470 INDIC1000,1)=1
0480 INDIC1000,2)=J
0490 INDIC1000,3)=K
0500 INDIC1000,4)=L
0510 INDIC1000,5)=R
0520 INDIC1000,6)=N
0530 INDIC1000,7)= 11
0540 INDIC1000,8)= J,J
0550 INDIC1000,9)= KK
0560 1.3 COST(IND)=C(I,1)+C(2,J)+C(3,K)+C(4,L)+C(5,M)+C(6,N)
0570 ↑ COST(I,1)+C(N,J)+C(K,K)
0580 8 EXPECT = EXPECT + (PROB(IND)*COST(I,IND))
0590 VAR = VAR + (PROB(IND)*COST(I,IND))
0600 10 CONTINUE

```

```

0610      IVAL$IND
0620      VAR = VAR - (EXECER*2)
0630      STOREV = SORT(1,VAR)
0640      DO 20 J=1,IVAL-1
0650      JA=J+1
0660      DO 19 K=JA,IVAL
0670      IF((COST(J,J),LE,COST(K))GO TO 19
0680      TEMP=COST(J,J)
0690      COST(J)=COST(K)
0700      COST(K)=TEMP
0710      TEMP=PROB(J,J)
0720      PROB(J)=PROB(K)
0730      PROB(K)=TEMP
0740      GO TO 14 . 19 . 19 ) . 10PT
0750      DO 18 L=1,9
0760      K1=INDIC(L,L)
0770      INDIC(J,L)=INDIC(K,L)
0780      INDIC(K,L)=K1
0790      18  CONTINUE
0800      19  CONTINUE
0810      20  CONTINUE
0820      WRITE(21,9030) EXPFCT , VAR , STDDEV
0830      CUM=0.0
0840      IF ( IOPT .EQ. 1 ) WRITE ( 21 + 9020 ) ((J,J = 1 . 9)
0850      IF ( IOPT .NE. 1 ) WRITE ( 21 + 9050 )
0860      GO TO 150 . 30 . 70 ) . 10PT
0870      50  DO 40 I=1,IVAL
0880      CUM=CUM+PROB(I)
0890      40  WRITE(21,2) COST(I,I),PRnB(I),CUM,INDIC(I,1),
0900      INDIC(I,2),INDIC(I,3),INDIC(I,4),INDIC(I,5),INDIC(I,6),
0910      .INDIC(I,7),INDIC(I,8),INDIC(I,9)
0920      GO TO 78
0930      30  I = 0
0940      31  PTEMP = 0.0
0950      32  I = 1 + 1
0960      PTTEMP = PTTEMP + PRnB(I)
0970      33  IF ( IVAL - I ) 78 + 34 , 33
0980      34  IF ((COST(I,I)-Q).GT..00005) GO TO 32
0990      34  CUM = CUM + PTTEMP
1000      WRITE(21,9040) COST(I,I),PTTEMP,CUM
1010      35  IF ( IVAL - I ) 78 + 78 + 31
1020      7C 0 . -0.5
1030      1 . 0
1040      71  PTTEMP = 0.0
1050      72  I = 0 + 1
1060      72  I = 1 + 1
1070      72  IF ((COST(I,I)-Q).GT..00005) GO TO 75
1080      73  PTTEMP = PTTEMP + PRnB(I)
1090      73  IF ( I - IVAL ) 76 + 77 + 78
1100      75  I = 0 + 1.0
1110      60  TO 73
1120      76  IF ((COST(I,I)-Q).LE..00005) GO TO 72
1130      77  CUM = CUM + PTTEMP
1140      78  Z = 0 . 0.5
1150      WRITE(21,9040) Z,PTTEMP,CUM
1160      79  IF ( I - IVAL ) 71 + 78 + 78
1170      79  CALL APPEND(21,WCSDP$,L,WCZKEY$20,WA3A " )
1180      CALL DETACH(21,1STAT,1)
1190      21  FORMAT(7F6.1,X,F10.6,7X,II,6IX,III)
1200      20 10 FORMAT(5,12,73,FA,2,755,F1,2,T185,FA,2,T13,F4,2)

```

```

1210 9020 FORMAT("1",//,T54,MN 1 STR 1 B U T 1 0 N",//,/)
1220   6   AT60,MA C T I V I T Y S T A T U S",/
1230   6   *T9,"COS1",T11,"PROBABILITY",T32,"CUMULATIVE"
1240   6   *T54,MN 1 = TYPE A IMPACT, 2 = TYPE A AND B IMPACTS,*"
1250   4   *T3 = NO IMPACT(1), /,T32,"PROBABILITY"
1260   4   *T6X,"FACT-",11,1),/
1270 9030 FORMAT(//,T12,"MEAN OF DISTRIBUTION",5X,F7.4,/,/
1280   8   *T12,"VARIANCE OF DISTRIBUTION",5X,F10.6,/,/
1290   4   *T12,"STANDARD DEVIATION OF DISTRIBUTION",5X,F10.4)
1300 9040 FORMAT(T4,F6.,1X,F10.6,F10.3),
1310 9050 FORMAT("1",//,T51,MN 1 STR 1 B U T 1 0 N",//,/,/
1320   4   *T49,"COST",4X,"PROBABILITY",4X,"CUMULATIVE",/
1330   8   *T72,"PROBABILITY")
1340 9060 FORMAT("1",//,T49,"TRACE RISK TABULATION DISTRIBUTION",/,/
1350   8   *T50,I N P U T ,P A R A E T R S",/,/
1360   6   *T12,"ACTIVITY",T29,"PROBABILITY OF",T55,"COST OF"
1370   6   *T74,"CONDITIONAL PROBABILITY OF",T112,"COST OF",/
1380   4   *T72,"TYPE A IMPACT",T52,"TYPE A IMPACT"
1390   4   *T80,"TYPE B IMPACT",T109,"TYPE B IMPACT",/,)
1400 STOP
1410 END

```

ANNEX C

## TRACE RISK FORMULATION DISTRIBUTION

## INPUT PARAMETERS

ACTIVITY	PROBABILITY OF TYPE A IMPACT	COST OF TYPE A IMPACT		CONDITIONAL PROBABILITY OF TYPE B IMPACT	COST OF TYPE B IMPACT	TYPE B IMPACT
		0.20	3.00			
1	0.60	0.40	0.00	1.00	1.00	1.00
2	0.25	0.80	0.00	0.00	0.00	0.00
3	0.60	1.50	0.75	0.75	4.00	4.00
4	0.20	0.50	1.00	1.00	0.50	0.50
5	0.75	0.20	1.00	1.00	2.00	2.00
6	0.70	0.00	1.00	1.00	6.00	6.00
7	0.60	0.00	1.00	1.00	2.50	2.50
8	0.30	0.00	1.00	1.00	4.00	4.00
9						

MEAN OF DISTRIBUTION 13.0000

VARIANCE OF DISTRIBUTION 22.177909

STANDARD DEVIATION OF DISTRIBUTION 4.709343

DISTRIBUTION

## DISTRIBUTION

COST	PROBABILITY	CUMULATIVE PROBABILITY	ACTIVITY STATUS									COST
			ACT-1	ACT-2	ACT-3	ACT-4	ACT-5	ACT-6	ACT-7	ACT-8	ACT-9	
0.	0.001613	0.001613	3	3	3	3	3	3	3	3	3	3
0.6	0.000539	0.002150	3	3	3	3	3	3	3	3	3	3
1.0	0.000403	0.002554	3	3	3	3	3	3	3	3	3	3
1.4	0.0002419	0.004973	3	3	3	3	3	3	3	3	3	3
1.8	0.000605	0.005578	3	3	3	3	3	3	3	3	3	3
2.2	0.000134	0.005712	3	3	3	3	3	3	3	3	3	3
2.4	0.0004819	0.010550	3	3	3	3	3	3	3	3	3	3
2.8	0.000806	0.011357	3	3	3	3	3	3	3	3	3	3
3.0	0.000202	0.011558	3	3	3	3	3	3	3	3	3	3
3.4	0.000605	0.012163	3	3	3	3	3	3	3	3	3	3
3.8	0.002419	0.014582	3	3	3	3	3	3	3	3	3	3
4.0	0.000151	0.014734	3	3	3	3	3	3	3	3	3	3
4.4	0.000907	0.015641	3	3	3	3	3	3	3	3	3	3
4.8	0.001613	0.017254	3	3	3	3	3	3	3	3	3	3
5.0	0.000403	0.017657	3	3	3	3	3	3	3	3	3	3
5.4	0.001210	0.018866	3	3	3	3	3	3	3	3	3	3
5.8	0.000202	0.019266	3	3	3	3	3	3	3	3	3	3
6.2	0.000050	0.019118	3	3	3	3	3	3	3	3	3	3
6.6	0.000806	0.019925	3	3	3	3	3	3	3	3	3	3
7.0	0.000605	0.020530	3	3	3	3	3	3	3	3	3	3
7.4	0.007258	0.027787	3	3	3	3	3	3	3	3	3	3
7.8	0.001914	0.029602	3	3	3	3	3	3	3	3	3	3
8.2	0.000302	0.029904	3	3	3	3	3	3	3	3	3	3
8.6	0.00174	0.030038	3	3	3	3	3	3	3	3	3	3
9.0	0.00227	0.030265	3	3	3	3	3	3	3	3	3	3
9.4	0.003629	0.033894	3	3	3	3	3	3	3	3	3	3
9.8	0.000402	0.034297	3	3	3	3	3	3	3	3	3	3
10.0	0.002097	0.035204	3	3	3	3	3	3	3	3	3	3
10.4	0.000691	0.035896	3	3	3	3	3	3	3	3	3	3
10.8	0.00101	0.035996	3	3	3	3	3	3	3	3	3	3
11.2	0.00202	0.036198	3	3	3	3	3	3	3	3	3	3
11.6	0.000605	0.036803	3	3	3	3	3	3	3	3	3	3
12.0	0.002415	0.039222	3	3	3	3	3	3	3	3	3	3
12.4	0.00151	0.039373	3	3	3	3	3	3	3	3	3	3
12.8	0.000605	0.039978	3	3	3	3	3	3	3	3	3	3
13.2	0.001815	0.041792	3	3	3	3	3	3	3	3	3	3
13.6	0.000559	0.042246	3	3	3	3	3	3	3	3	3	3
14.0	0.007258	0.049504	3	3	3	3	3	3	3	3	3	3
14.4	0.00016	0.049579	3	3	3	3	3	3	3	3	3	3
14.8	0.001210	0.050780	3	3	3	3	3	3	3	3	3	3
15.2	0.000230	0.051019	3	3	3	3	3	3	3	3	3	3
15.6	0.00034	0.051053	3	3	3	3	3	3	3	3	3	3
16.0	0.000302	0.051355	3	3	3	3	3	3	3	3	3	3
16.4	0.000907	0.052262	3	3	3	3	3	3	3	3	3	3
16.8	0.002027	0.052489	3	3	3	3	3	3	3	3	3	3
17.2	0.00173	0.052662	3	3	3	3	3	3	3	3	3	3
17.6	0.002722	0.055384	3	3	3	3	3	3	3	3	3	3
18.0	0.001210	0.055593	3	3	3	3	3	3	3	3	3	3
18.4	0.000202	0.056795	3	3	3	3	3	3	3	3	3	3
18.8	0.00050	0.056645	3	3	3	3	3	3	3	3	3	3
19.2	3.001G37	0.057882	3	3	3	3	3	3	3	3	3	3

5.4	0.000151	0.050333
5.4	0.000605	0.058638
5.4	0.001361	0.059999
5.5	0.000259	0.060558
5.5	0.000151	0.060400
5.5	0.001814	0.062224
5.5	0.000605	0.06292H
5.5	0.002419	0.065248
5.5	0.000038	0.065285
5.5	0.001814	0.067100
5.7	0.000302	0.067002
5.7	0.000076	0.067478
5.8	0.000058	0.067535
5.9	0.000907	0.084031
5.9	0.000227	0.086659
6.0	0.003763	0.072334
6.0	0.000403	0.072836
6.1	0.000680	0.073516
6.1	0.010886	0.084403
6.2	0.002707	0.086476
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6.3	0.000013	0.091169
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6.4	0.000259	0.091853
6.5	0.000151	0.092006
6.5	0.000137	0.093043
6.5	0.000655	0.093107
6.5	0.000454	0.093561
6.5	0.000605	0.094166
6.6	0.001814	0.095980
6.6	0.000454	0.096434
6.7	0.00076	0.096509
6.8	0.001254	0.097764
6.9	0.000227	0.097991
7.0	0.000272	0.100712
7.0	0.000057	0.100769
7.0	0.000691	0.104398
7.0	0.000907	0.105307
7.0	0.000227	0.105694
7.0	0.000389	0.106635
7.0	0.000941	0.109791
7.1	0.000101	0.106735
7.1	0.000272	0.111455
7.2	0.000518	0.111973
7.2	0.000680	0.112654
7.2	0.000113	0.112767
7.2	0.000086	0.112854
7.3	0.000050	0.112904
7.3	0.000346	0.113295
7.3	0.000022	0.113277

5.4	0.0000151	0.0000605	0.001361	0.0002559	0.0002155	0.0001814	0.0000605	0.0004419	0.0000388	0.0001814	0.0000302	0.0000680	0.000058	0.0000907	0.0002272	0.0003763	0.000403	0.0006880	0.0002746	0.0000500	0.000454	0.0000202	0.0000013	0.0000886	0.000340	0.0002559	0.000151	0.0001037	0.0000605	0.000454	0.000005	0.000151	0.000057	0.00003629	0.0000907	0.0002272	0.0000173	0.0000101	0.0000591	0.0000097	0.0000227	0.0000113	0.0000086	0.0000346	0.0000022
5.5	0.0000151	0.0000605	0.001361	0.0002559	0.0002155	0.0001814	0.0000605	0.0004419	0.0000388	0.0001814	0.0000302	0.0000680	0.000058	0.0000907	0.0002272	0.0003763	0.000403	0.0006880	0.0002746	0.0000500	0.000454	0.0000202	0.0000013	0.0000886	0.000340	0.0002559	0.000151	0.0001037	0.0000605	0.000454	0.000005	0.000151	0.000057	0.00003629	0.0000907	0.0002272	0.0000173	0.0000101	0.0000591	0.0000097	0.0000227	0.0000113	0.0000086	0.0000346	0.0000022
5.6	0.0000151	0.0000605	0.001361	0.0002559	0.0002155	0.0001814	0.0000605	0.0004419	0.0000388	0.0001814	0.0000302	0.0000680	0.000058	0.0000907	0.0002272	0.0003763	0.000403	0.0006880	0.0002746	0.0000500	0.000454	0.0000202	0.0000013	0.0000886	0.000340	0.0002559	0.000151	0.0001037	0.0000605	0.000454	0.000005	0.000151	0.000057	0.00003629	0.0000907	0.0002272	0.0000173	0.0000101	0.0000591	0.0000097	0.0000227	0.0000113	0.0000086	0.0000346	0.0000022
5.7	0.0000151	0.0000605	0.001361	0.0002559	0.0002155	0.0001814	0.0000605	0.0004419	0.0000388	0.0001814	0.0000302	0.0000680	0.000058	0.0000907	0.0002272	0.0003763	0.000403	0.0006880	0.0002746	0.0000500	0.000454	0.0000202	0.0000013	0.0000886	0.000340	0.0002559	0.000151	0.0001037	0.0000605	0.000454	0.000005	0.000151	0.000057	0.00003629	0.0000907	0.0002272	0.0000173	0.0000101	0.0000591	0.0000097	0.0000227	0.0000113	0.0000086	0.0000346	0.0000022

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7.4	0.005645	0.1119672
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7.6	0.000454	0.121947
7.6	0.000310	0.125058
7.6	0.000082	0.129140
7.7	0.001814	0.130954
7.7	0.000778	0.131732
7.7	0.005443	0.137115
7.7	0.000113	0.137289
7.8	0.000076	0.138780
7.8	0.000130	0.137418
7.8	0.000032	0.137721
7.9	0.001555	0.140659
7.9	0.000907	0.138658
7.9	0.000097	0.137152
7.9	0.000680	0.141226
7.9	0.000907	0.142333
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8.0	0.002722	0.145582
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8.0	0.000173	0.145681
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8.0	0.000043	0.145181
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8.1	0.000080	0.146651
8.1	0.001882	0.148732
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10.7	0.0001361	0.321834	3
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10.9	0.000117	0.325661	1
10.9	0.000189	0.32674	1
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11.0	0.000529	0.330791	3
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11.0	0.000170	0.331277	1
11.0	0.000369	0.331334	3
11.0	0.000057	0.331737	3
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-9	0.001588	0.426578
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13.9	0.000176	0.555418
13.7	0.000529	0.565948
13.9	0.00024	0.565972
13.9	0.002117	0.566089
13.9	0.001165	0.569255
14.0	0.000132	0.569387
14.0	0.000101	0.571425
14.0	0.0006240	0.571775
14.0	0.0006680	0.578456
14.1	0.000875	0.579331
14.1	0.001598	0.580918
14.1	0.000577	0.581210
14.2	0.000012	0.581222
14.2	0.000583	0.581805
14.2	0.000499	0.583204
14.2	0.000085	0.583389
14.2	0.000510	0.583900

	0.000773	0.585971
14.3	0.000053	0.586173
14.3	0.000016	0.586190
14.3	0.000194	0.586986
14.4	0.002119	0.589403
14.4	0.003175	0.592573
14.4	0.000037	0.593016
14.4	0.000053	0.593358
14.4	0.000605	0.593971
14.5	0.001111	0.595385
14.5	0.000088	0.595473
14.5	0.000151	0.595622
14.5	0.00005	0.596229
14.5	0.000234	0.600463
14.5	0.000158	0.601521
14.6	0.000281	0.603902
14.6	0.000114	0.605717
14.6	0.000037	0.606156
14.6	0.000352	0.606216
14.7	0.000056	0.610273
14.7	0.000151	0.610728
14.7	0.000242	0.611938
14.7	0.000183	0.612521
14.7	0.000258	0.619778
14.7	0.000000	0.619876
14.7	0.000175	0.623051
14.7	0.000176	0.623221
14.7	0.000076	0.623303
14.7	0.000529	0.623932
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14.7	0.000044	0.625993
14.8	0.000302	0.626295
14.8	0.000034	0.626320
14.9	0.000097	0.627236
14.9	0.000529	0.627765
14.9	0.000073	0.627838
14.9	0.000292	0.628130
14.9	0.000087	0.628217
15.0	0.000292	0.628519
15.0	0.001166	0.529685
15.0	0.0001588	0.631211
15.0	0.000073	0.631297
15.0	0.000224	0.631520
15.0	0.000027	0.631693
15.0	0.000170	0.631693
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15.1	0.000097	0.638441
15.1	0.019051	0.657492
15.1	0.001210	0.664233
15.1	0.000225	0.664498
15.1	0.000116	0.660360
15.2	0.000352	0.564851
15.2	0.000202	0.660561
15.2	0.000050	0.664901
15.2	0.001361	0.666262
15.2	0.000526	0.675780
15.3	0.000046	0.675933
15.3	0.0000794	0.6777727

0.000198

0.476926

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$\sigma$	$\sigma_{\text{min}}$	$\sigma_{\text{max}}$	$\sigma_{\text{mean}}$	$\sigma_{\text{std}}$
15.4	0.001021	0.677946	0.677946	0.677946
15.4	0.000605	0.677551	0.677551	0.677551
15.4	0.002051	0.678702	0.678702	0.678702
15.4	0.000353	0.679055	0.679055	0.679055
15.4	0.000151	0.679306	0.679306	0.679306
15.5	0.000605	0.67811	0.67811	0.67811
15.5	0.001914	0.685626	0.685626	0.685626
15.5	0.002419	0.680045	0.680045	0.680045
15.5	0.000038	0.68401	0.68401	0.68401
15.5	0.001058	0.635	0.635	0.635
15.5	0.00025	0.685	0.685	0.685
15.5	0.000194	0.690058	0.690058	0.690058
15.5	0.000116	0.693086	0.693086	0.693086
15.5	0.000076	0.694108	0.694108	0.694108
15.5	0.000529	0.694183	0.694183	0.694183
15.5	0.002111	0.694712	0.694712	0.694712
15.5	0.000112	0.698961	0.698961	0.698961
15.5	0.000227	0.697188	0.697188	0.697188
15.5	0.000159	0.698176	0.698176	0.698176
15.5	0.0003907	0.699583	0.699583	0.699583
15.5	0.0005350	0.700633	0.700633	0.700633
15.5	0.000073	0.706116	0.706116	0.706116
15.5	0.000403	0.706110	0.706110	0.706110
15.5	0.000528	0.707039	0.707039	0.707039
15.5	0.000292	0.707330	0.707330	0.707330
15.5	0.000875	0.708005	0.708005	0.708005
15.5	0.010886	0.710092	0.710092	0.710092
15.5	0.000680	0.715772	0.715772	0.715772
15.5	0.004763	0.724535	0.724535	0.724535
15.5	0.011588	0.726122	0.726122	0.726122
15.5	0.001175	0.72927	0.72927	0.72927
15.5	0.005154	0.729751	0.729751	0.729751
15.5	0.009302	0.730014	0.730014	0.730014
15.5	0.019051	0.749105	0.749105	0.749105
15.5	0.000659	0.749155	0.749155	0.749155
15.5	0.007722	0.751877	0.751877	0.751877
15.5	0.000056	0.751943	0.751943	0.751943
15.5	0.001367	0.752310	0.752310	0.752310
15.5	0.005650	0.752916	0.752916	0.752916
15.5	0.000232	0.753145	0.753145	0.753145
15.5	0.000084	0.753214	0.753214	0.753214
15.5	0.005013	0.75347	0.75347	0.75347
15.5	0.000255	0.753502	0.753502	0.753502
15.5	0.003340	0.75356	0.75356	0.75356
15.5	0.000137	0.754450	0.754450	0.754450
15.5	0.000381	0.755661	0.755661	0.755661
15.5	0.001759	0.75611	0.75611	0.75611
15.5	0.000036	0.758447	0.758447	0.758447
15.5	0.000454	0.758901	0.758901	0.758901
15.5	0.000151	0.759952	0.759952	0.759952
15.5	0.000054	0.759975	0.759975	0.759975
15.5	0.000049	0.759975	0.759975	0.759975

16.5	0.00131?	0.751018
16.5	0.00201	0.763399
16.5	0.001814	0.763213
16.5	0.003175	0.768389
16.7	0.000454	0.768442
16.7	0.000076	0.758918
16.7	0.000529	0.769447
16.8	0.000674	0.769471
16.8	0.001588	0.771059
16.9	0.000907	0.771966
16.9	0.003097	0.772363
16.9	0.000227	0.772590
16.9	0.000657	0.772647
16.9	0.000533	0.773176
16.9	0.002722	0.775897
16.9	0.000292	0.776180
16.9	0.0003629	0.779318
17.0	0.001588	0.781405
17.0	0.000132	0.781538
17.0	0.000272	0.781764
17.0	0.000090	0.782372
17.0	0.000101	0.792772
17.0	0.000635	0.7949123
17.1	0.000219	0.789341
17.1	0.000132	0.792063
17.2	0.000660	0.792243
17.2	0.000076	0.793337
17.2	0.0004763	0.794800
17.2	0.000113	0.798813
17.2	0.000146	0.799559
17.2	0.000875	0.799634
17.3	0.000050	0.799984
17.3	0.000151	0.799984
17.4	0.000109	0.799745
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17.4	0.000605	0.800187
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17.9	0.000227	0.846856
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17.9	0.000680	0.847009
17.9	0.000907	0.848116
18.0	0.000227	0.851238
18.0	0.000057	0.851522

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18.0

0.001588  
0.000397

0.853109  
0.853104

16.0	0.001589	0.853100
16.0	0.001397	0.853798
16.0	0.001326	0.854478
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16.1	0.000763	0.855241
16.2	0.000026	0.859277
16.2	0.000219	0.859496
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16.4	0.001361	0.861197
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16.5	0.000605	0.874550
16.5	0.0009526	0.879874
16.5	0.002381	0.873255
16.5	0.000199	0.873454
16.5	0.000454	0.873907
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16.6	0.000714	0.886106
16.6	0.001361	0.887467
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16.7	0.000076	0.887634
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16.7	0.0001021	0.877640
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16.8	0.000132	0.888374
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16.9	0.000188	0.880669
16.9	0.000227	0.881096
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16.9	0.000073	0.891846
17.0	0.0001191	0.89304C
17.1	0.000715	0.901204
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17.6	0.0002722	0.922514
17.6	0.000680	0.923194
17.7	0.000907	0.924102
17.7	0.000057	0.92415R
17.7	0.000397	0.924555
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17.8	0.001588	0.926370
17.8	0.002041	0.929411
17.9	0.000227	0.927222
17.9	0.000680	0.928194
17.9	0.000907	0.929102
17.9	0.000057	0.92915R
17.9	0.000397	0.929411
18.0	0.000227	0.929411

0.0006680	0.929091
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20.2	0.000170
20.2	0.000198
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20.4	0.001021
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20.5	0.007144
20.6	0.001021
20.7	0.0001361
20.7	0.000227
20.8	0.000227
20.9	0.000170
20.9	0.000589
21.0	0.000057
21.0	0.002722
21.0	0.000340
21.0	0.00054
21.0	0.000397
21.1	0.002041
21.2	0.000340
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21.3	0.000340
21.4	0.000057
21.5	0.000340
21.6	0.000227
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21.7	0.001786
21.7	0.000290
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21.8	0.000057
21.8	0.000227
21.9	0.000121
22.0	0.000680
22.0	0.000170
22.1	0.0002041
22.1	0.000290
22.2	0.000055
22.2	0.000082
22.3	0.000121
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23.2	0.000340
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23.3	0.000113
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23.5	0.000055
23.6	0.000340
23.7	0.000170
23.8	0.000680
24.0	0.000510
24.1	0.000095
24.2	0.0002041
24.3	0.000121
24.4	0.000082
24.5	0.003062
24.6	0.0001021
24.7	0.000055
24.8	0.000340
24.9	0.000170
25.0	0.000680
25.1	0.000510
25.2	0.0002041
25.3	0.000113
25.4	0.0002041
25.5	0.000095
25.6	0.000340
25.7	0.000170
25.8	0.000680
25.9	0.000510
26.0	0.0002041
26.1	0.000113
26.2	0.0002041
26.3	0.000095
26.4	0.000340

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